A Computational Model of the Human Left-Ventricular Epicardial Myocyte

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ABSTRACT   A computational model of the human left-ventricular epicardial myocyte is presented. Models of each of the major ionic currents present in these cells are formulated and validated using experimental data obtained from studies of recombinant human ion channels and/or whole-cell recording from single myocytes isolated from human left-ventricular subepicardium. Continuous-time Markov chain models for the gating of the fast Na^+ current, transient outward current, rapid component of the delayed rectifier current, and the L-type calcium current are modified to represent human data at physiological temperature. A new model for the gating of the slow component of the delayed rectifier current is formulated and validated against experimental data. Properties of calcium handling and exchanger currents are altered to appropriately represent the dynamics of intracellular ion concentrations. The model is able to both reproduce and predict a wide range of behaviors observed experimentally including action potential morphology, ionic currents, intracellular calcium transients, frequency dependence of action-potential duration, Ca^{2+}-frequency relations, and extrasystolic restitution/post-extrasystolic potentiation. The model therefore serves as a useful tool for investigating mechanisms of arrhythmia and consequences of drug-channel interactions in the human left-ventricular myocyte.

INTRODUCTION

Computational models of the mammalian ventricular myocyte have become important tools for understanding the biophysical basis of the ventricular action potential (AP), for relating changes in gene/protein expression and effects of gene mutations to alterations of AP and calcium (Ca^{2+}) transient morphology, and for investigating mechanisms of arrhythmia (Clancy and Rudy, 1999; Luo and Rudy, 1991, 1994; Noble et al., 1998; Pandit et al., 2001; Winslow et al., 1999). These models describe properties of voltage-gated ionic currents, membrane pumps and exchangers, intracellular Ca^{2+} cycling, Ca^{2+}-induced Ca^{2+}-release, and processes regulating intracellular sodium (Na^+) and potassium (K^+) concentrations. Models of ventricular myocytes isolated from guinea pig (Luo and Rudy, 1994; Noble et al., 1998), rat (Pandit et al., 2001), canine (Winslow et al., 1999), and human (Priebe and Beuckelmann, 1998) heart have been developed.

The Priebe-Beuckelmann model and simplifications thereof (Bernus et al., 2002) are the first human ventricular myocyte models developed and were derived via parameter variation from the Luo-Rudy phase II ventricular myocyte model. Ten Tusscher et al. (2003) subsequently presented a human myocyte model in which properties of membrane currents are based on more recent whole-cell current data measured in isolated human ventricular myocytes. Each of these models is able to reconstruct qualitative features of AP and Ca^{2+} transient morphology; however, they make limited use of what is now substantial experimental data on properties of both wild-type and recombinant channels, whole-cell currents, excitation-contraction coupling processes, and processes regulating intracellular Na^+ concentration (Na_i) in the human ventricular myocyte. The model described here is based on these more extensive experimental data.

The resulting myocyte model exhibits long-term stability of intracellular ion concentrations over a range of pacing frequencies and is able to reproduce and predict diverse behaviors measured experimentally in isolated human ventricular myocytes including: 1), properties of voltage-dependent ionic currents; 2), AP morphology and rate-dependent changes of AP duration (APD); 3), Ca^{2+}-transient morphology and Ca^{2+}-frequency relations; and 4), properties of extrasystolic restitution and post-extrasystolic potentiation.

METHODS

Model development

The human myocyte model consists of a system of ordinary differential-algebraic equations describing the time-rate of change of channel-state occupancy probabilities and intracellular concentrations of Na^+, K^+, and Ca^{2+}, whole-cell current through ion channels, membrane pumps and exchangers, and the dynamics of intracellular Ca^{2+} cycling processes. Complete model equations and parameters are given in the Appendix.

Fast inward Na^+ current (I_{Na})

I_{Na} is modeled based on the formulation of Irvine et al. (1999). This model is constrained by single channel and whole-cell measurements of recombinant

cardiac hH_1 channels, and is able to reproduce diverse experimental data including ionic currents, gating currents, tail currents, steady-state inactivation, recovery from inactivation, and single channel open time distribution. Model state transition rates are explicit functions of enthalpy, entropy, voltage, and temperature. The original model behavior has been verified over the temperature range of 10°–23°C, but does not extrapolate directly to body temperature. Model parameters are therefore adjusted in this work to match Na^+ current dynamics at physiologic temperature (Nagatomo et al., 1998; Wang et al., 2000). Analytical methods used to extrapolate I_{Na} to 33°C are given in the Appendix. The I_{Na} density is also adjusted to reproduce measurements of AP amplitude (Li et al., 1998; Nabauer et al., 1996) and phase 0 upstroke velocity (V_{max}) measured experimentally in human ventricular subepicardium and midmyocardium (Drouin et al., 1995; Pereon et al., 2000). Model AP amplitude is 126 mV at 1 Hz pacing, which is in the midrange of experimental measurements (100 mV, Li et al., 1999; 132 mV, Li et al., 1998; and 135 mV, Nabauer et al., 1996). Model V_{max} is 350 V/s (experimental measurements range from 228 ± 20 V/s, Drouin et al., 1995, to 446 ± 46 V/s, Pereon et al., 2000).

Simulated behavior of I_{Na} is compared with experimental data from recombinant human hH_1 channels in Fig. 1. Data on activation, inactivation, and recovery from inactivation largely fall within the experimental error bars. Simulated steady-state activation and inactivation functions are in agreement with experimental data, having a half-maximal activation voltage of −39.6 mV and slope factor 7.2 (compared with measurements of −39.6 ± 2.2 mV and 7.1 ± 0.5; Nagatomo et al., 1998), and half-maximal inactivation voltage of −82.4 mV and slope factor 5.8 (compared with measurements of −85.8 ± 2.7 and 5.8 ± 0.1; Nagatomo et al., 1998).

Delayed rectifier K$^+$ currents (I_{Kr} and I_{Ks})

In human left ventricle, the delayed rectifier current (I_K) consists of two components-a rapidly activating and inactivating component (I_{Kr}) and a slowly activating component (I_{Ks}) (Iost et al., 1998; Li et al., 1996). A model for human I_{Kr} was developed recently by Mazhari et al. (2001) based on recordings from recombinant co-assembled human KCNH2/KCNE2 channels. This model has been shown to reproduce a broad range of I_{Kr} current characteristics and was incorporated without change into the human whole-cell model. I_{Kr} conductance was set to 0.0186 mS/μF to match recordings in isolated human ventricular myocytes (Magyar et al., 2000).

Recent studies of recombinant co-assembled human KCNQ1/KCNE1 channels, which likely encode I_{Ks}, have revealed details on its gating structure (Pusch, 1998; Pusch et al., 2000, 2001, 1998; Tristani-Firouzi and Sanguinetti, 1998). Based on this evidence, a Markov model for the gating of
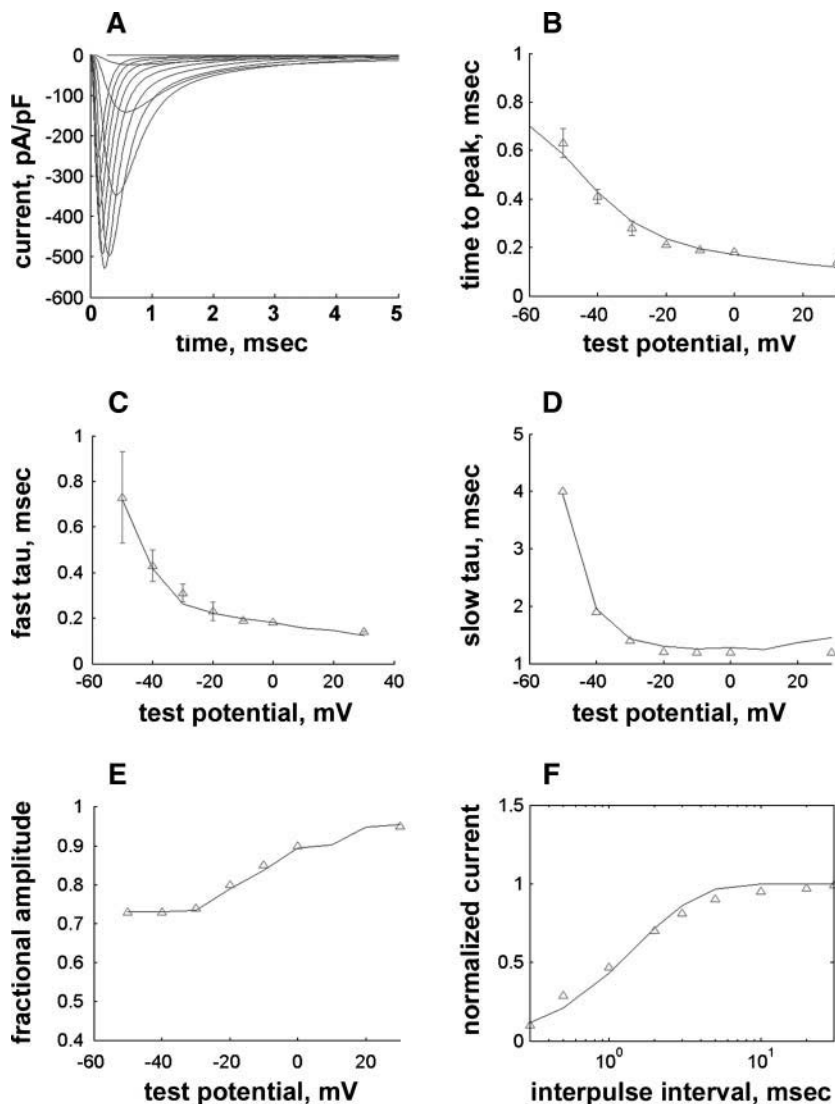

FIGURE 1 Comparison of simulated (*solid line*) versus experimentally measured properties, from Nagatomo et al. (1998) and Wang et al. (2000), of I_{Na} (△) at 33°C. (*A*) Model voltage-clamp current responses compared with experimental data (△) over the range −50 mV to +30 mV. Activation and inactivation kinetics were studied using a voltage-clamp protocol with a holding potential of −150 mV and steps of 24-mS duration to various depolarizing potentials at 33°C. (*B*) Comparison of time to peak current (ordinate, ms) as a function of test potential (abscissa, mV) for model versus experiments; see Fig 3, *B–E*, in Nagatomo et al. (1998). (*C*) The decay phase of the current traces at potentials from −50 mV to +30 mV was fit with a sum of two weighted exponentials. *C* shows the fast time constant of inactivation (ordinate, ms) plotted against test potential (abscissa, mV). (*D*) Slow time constant of inactivation (ordinate, ms) plotted against test potential (abscissa, mV) from fitting procedure described in *C*. (*E*) Fractional amplitude of the fast component of inactivation (ordinate) plotted against test potential (abscissa, mV) from fitting procedure described in *C*. (*F*) Time course of recovery from inactivation expressed as fraction of maximum current (ordinate) versus recovery interval (abscissa, ms). Data obtained using a two-pulse protocol with a variable interpulse recovery interval (abscissa). Current in second pulse was normalized to current in first pulse and plotted as the ordinate. Experimental data provided for comparison from Fig. 4 in Wang et al. (2000).

I_{Ks} channels is used. This model incorporates four sequential states (C_1–C_2–O_3–O_4), two of which are nonconducting (C_1 and C_2), followed by two open, conducting states (O_3 and O_4). Two open states are included on the basis of experiments in co-assembled KCNQ1/KCNE1 channels: 1), Pusch et al. (2001) deduced two conducting states with differential sensitivity to intracellular Na^+ block; and 2), Pusch et al. (2001) recorded a sigmoidal tail current decay characteristic of two open states in the presence of extracellular rubidium (which interferes with and slows channel deactivation). Initially, four closed states were included in the model to reflect the tetrameric structure of the channel. However, to simplify the model, the rapid equilibrium approximation (Hille, 1972) was used to lump the three rapid closed-state transitions into a single activation step (C_1–C_2), followed by gating into conducting states (C_2 to O_3 and O_3 to O_4). This resulted in no significant change in the ability of the model to fit experimental data.

Although studies have reported difficulty in isolating I_{Ks} in human myocardium (Veldkamp, 1998), recent experiments have established the presence of this current in human left (Virág et al., 2001) and right (Li et al., 1996) ventricle. The data of Virág et al. (2001) are used to constrain activation and deactivation properties of the channel model. Constraining data include tail current magnitudes, responses to an envelope of tails protocol, activation time constants, and deactivation time constants. The whole-cell conductance of I_{Ks} was set to 0.0035 mS/μF to match tail current magnitudes measured in human ventricle (Magyar et al., 2000; Virág et al., 2001). Comparison of model I_{Ks} behavior with experimental data is provided in Fig. 2.

Transient outward Ca^{2+}-independent K^+ current (I_{to1})

In human ventricle, I_{to1} consists of two components. $I_{to1,f}$ is likely encoded by KCND3 and exhibits fast recovery from inactivation (Dixon et al., 1996). $I_{to1,s}$ is likely encoded by KCNA4 and exhibits relatively slow kinetics of recovery from inactivation (Po et al., 1992). Continuous-time Markov chain models for the gating of human KCND3 and KCNA4 channels have been developed by Greenstein et al. (2000) and have been shown to reproduce human I_{to1} current properties accurately. These models are incorporated into the human myocyte model. The fast recovery component, which comprises 89% of human I_{to1} (Nabauer et al., 1996), was implemented without adjustment. The slowly recovering component was implemented with one modification—changing the time constant of inactivation to 45 ms for potentials between -10 mV and $+40$ mV (Nabauer et al., 1996). Density of I_{to1} was adjusted to a value of 10 pA/pF in response to a voltage-clamp step to $+60$ mV from a holding potential of -80 mV, corresponding to experimental measurements in human ventricular subepicardium (Konarzewska et al., 1995; Nabauer et al., 1996; Wettwer et al., 1998).

Inward rectifier K^+ current (I_{K1})

In human ventricle, I_{K1} activates with a half-maximal activation voltage equal to the reversal potential for K^+ (Kubo and Murata, 2001), has a density proportional to the square-root of the extracellular K^+ concentration (Bailly
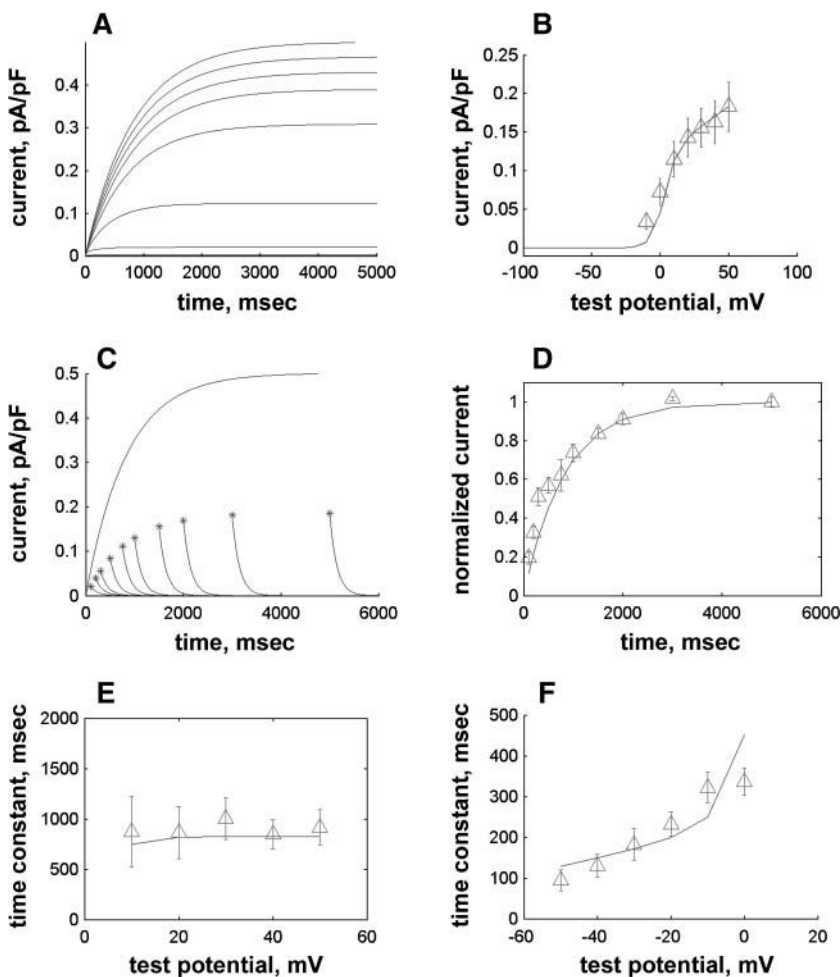

FIGURE 2 Comparison of simulated versus measured (Virág et al., 2001) I_{Ks} properties. (*A*) Simulated I_{Ks} in response to voltage-clamp steps from a holding potential of -40 mV to potentials from -10 mV to 50 mV. (*B*) Tail current magnitudes at -40 mV (ordinate, pA/pF) were computed after depolarization to test potentials (abscissa, mV) from -10 mV to 50 mV for 5000 ms. Experimental tail current magnitudes provided for comparison; from Fig. 2 *C*, in Virág et al. (2001). (*C*) Envelope of tails protocol. Voltage-clamp step to $+50$ mV of varying duration was followed by return to holding potential. Resultant tail currents (ordinate, pA/pF) plotted versus duration of voltage-clamp step (abscissa, ms), overlaid on step current. Peak tail currents are denoted by asterisks. (*D*) Normalized peak tail currents from protocol in *C* (ordinate), plotted versus voltage clamp duration (abscissa, ms), highlighting time course of activation of tail currents. Both model and experiment show a slowly activating outward current without evidence of inactivation at $+50$ mV. Experimental data from Fig. 3 in Virág et al. (2001). (*E*) Time constant of activation calculated from protocol in *D* (ordinate, ms), computed for step potentials from $+10$ to $+50$ mV (abscissa, mV). Data from Fig. 4 in Virág et al. (2001). (*F*) Kinetics of deactivation. Tail currents were elicited at potentials between -50 mV and 0 mV and the decay phase was fit with a single exponential. Deactivation time constants (ordinate, ms) were calculated and compared with experimental findings as a function of step potential (abscissa, mV). Experimental data from Fig. 4 in Virág et al. (2001).

et al., 1998), and gates sufficiently fast over physiologic potentials for gating kinetics to be considered instantaneous (Koumi et al., 1995). Thus, activation curves for I_{K1} were modeled as instantaneous functions of voltage, and current density was set to be a function of the square-root of extracellular potassium. The formulation for I_{K1} thus becomes (complete equations and parameter values given in Appendix)

$$I_{K1}(V, K_o) = G_{K1}\sqrt{K_o}K1_{\text{open}}(V)[V - E_{K1}], \quad (1)$$

$$K1_{\text{open}}(V) = \frac{1}{k_1 + \exp\left(\dfrac{V - E_{K1}}{k_2}\right)}. \quad (2)$$

The voltage dependence of channel rectification ($K1_{\text{open}}$) was constrained using recordings from recombinant human KCNJ2 channels in *Xenopus* oocytes (Kubo and Murata, 2001), and current density (G_{K1}) was constrained using recordings of slope conductance in human left-ventricular subepicardial myocytes at different extracellular K^+ concentrations (Bailly et al., 1998). Properties of the model I_{K1} are compared with experimental data in Fig. 3.

L-type Ca²⁺ current (I_{CaL})

The formulation for I_{CaL} was adopted from Winslow et al. (1999). Rate constants were adjusted to represent the kinetics of inactivation and recovery from inactivation measured in human ventricular myocytes (Li et al., 1999; Magyar et al., 2002). Characteristics of steady-state inactivation were also modified to match experimental findings in human ventricle (Li et al., 1999). Whole-cell conductance was set to achieve a peak inward current density of -6 pA/pF in the presence of 10 mM EGTA, which is in the midrange of

values measured in human ventricle (Beuckelmann and Erdmann, 1992; Li et al., 1999; Magyar et al., 2002; Mewes and Ravens, 1994). Fig. 4 contrasts model versus experimental responses to voltage-clamp stimuli.

I_{NaCa} and I_{SERCA}

Sodium-calcium exchanger current (I_{NaCa}) is modeled after Winslow et al. (1999). I_{NaCa} current density in myocytes isolated from human left-ventricular subepicardium has been measured to be 0.54 ± 0.04 pA/pF at -40 mV; extracellular Na^+ and Ca^{2+} concentrations of 0 and 1 mM, respectively; pipette Na^+ concentration of 10 mM; and free Ca^{2+} at 100 nM (Su et al., 1999). Setting the current density scaling factor k_{NaCa} (see Appendix) to a value of 0.44 elicits a 0.54 pA/pF current density under these conditions.

The SR-Ca^{2+} ATPase current (I_{SERCA}) is constrained using data on the rate of decline of Ca^{2+} transients in voltage-clamped human ventricular myocytes in physiological and Na^+-free solutions (Beuckelmann et al., 1992, 1995). The decay kinetics of the Ca^{2+} transient are influenced by two major Ca^{2+} extrusion mechanisms-I_{NaCa} and I_{SERCA} (Bers, 2001). I_{SERCA} can be constrained by fixing I_{NaCa} density using the values estimated above, and then varying the magnitude of I_{SERCA} to match experimental Ca^{2+} transient decay rates. The I_{SERCA} scaling factor K_{SR} (see Appendix) was set to a value of 1.2 to reproduce two findings in human ventricular myocytes. A K_{SR} value of 1.2 produces a time to half-decay of the Ca^{2+} transient (from peak value) of 270 ms in 5 mm Na^+ (reported experimentally as 270 ms and 320 ± 68 ms; see Beuckelmann et al., 1992). I_{SERCA} was also estimated using data from experiments in which pipette and extracellular Na^+ concentrations were 0 mM (Beuckelmann et al., 1995), thus ablating I_{NaCa}. A model K_{SR} value of 1.25, in an I_{NaCa}-free simulation, yielded Ca^{2+} transient decay rates matching that measured experimentally (305 ± 16 ms). Since this independent estimate provided a similar value for K_{SR}, the original value of 1.2 is selected as the value for K_{SR} in the human model.
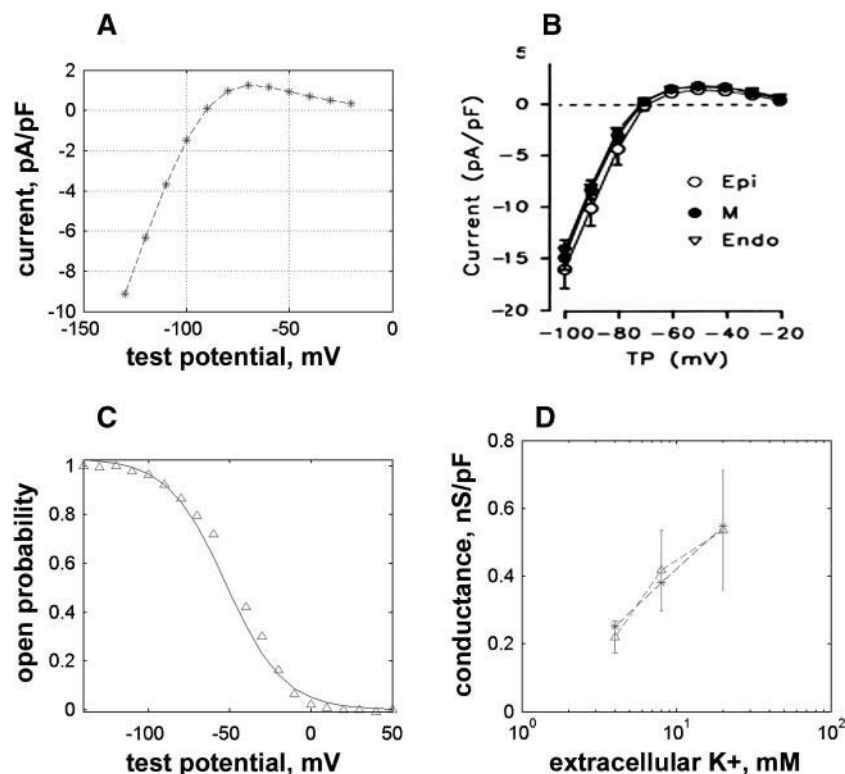

FIGURE 3 Comparison of simulated (*asterisk symbol*) versus measured ($\triangle$) (Bailly et al., 1998; Kubo and Murata, 2001) I_{K1} properties. (*A*) Steady-state current (ordinate, pA/pF) as a function of voltage (abscissa, mV), referred to as an I–V curve, computed by multiplying the activation curve *B* by whole-cell conductance and electrical driving force. (*B*) Experimental I–V curve from Fig. 3 in Li et al. (1998). (*C*) Steady-state open fraction (ordinate) as a function of membrane potential (abscissa, mV) for model I_{K1} overlaid with experimental measurements obtained from human KCNJ2 channels; from Fig. 2 *C* in Kubo and Murata (2001). (*D*) Open channel conductance (ordinate, mS/μF) as a function of extracellular K^+ concentration (abscissa, mV). Experimental data from Fig. 2 *C* in Bailly et al. (1998).
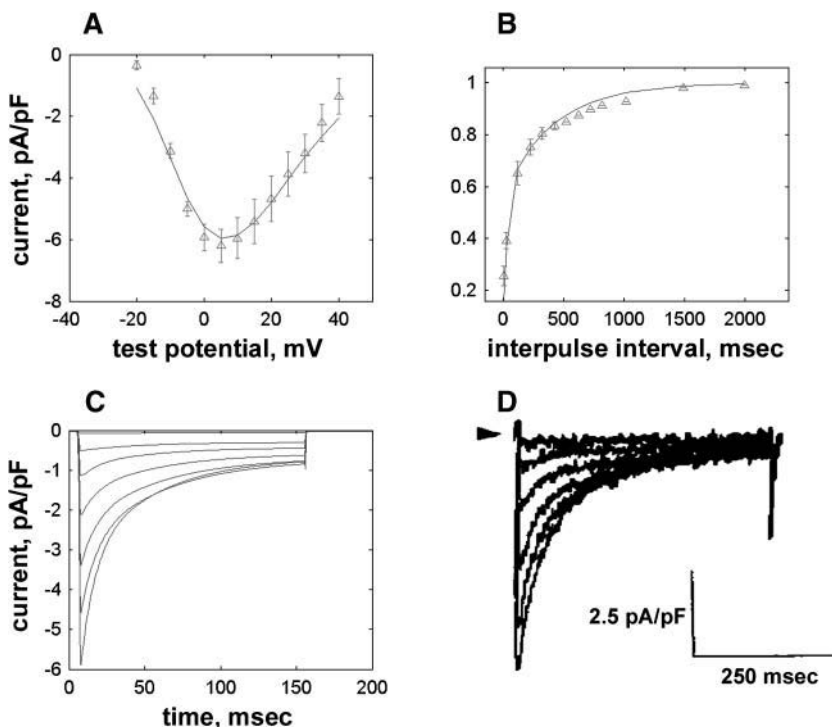
FIGURE 4 Comparison of model (*lines*) versus experimental ($\triangle$) (Li et al., 1999; Mewes and Ravens, 1994) I_{CaL} properties. Experiments and simulations were performed using 10 mM EGTA. (*A*) Normalized model peak I–V relation (holding potential −40 mV) contrasted with experimental data (from Fig. 6 *B* in Li et al., 1999). (*B*) Inactivation recovery properties assessed using a two pulse protocol with a variable interpulse interval at holding potential of −80 mV. Current in the second pulse is normalized to current in the first pulse (ordinate), and plotted as a function of interpulse interval (abscissa, ms). Experimental data from Fig. 5 *B* in Li et al. (1999). (*C*) Currents in response to voltage-clamp stimuli. From a holding potential of −40 mV, EGTA-loaded myocytes were depolarized from −35 mV to +5 mV. (*D*) Experimental family of voltage-clamp-elicited currents under same protocol as *C*, from Fig 4 *A* in Mewes and Ravens (1994).

Intracellular Na$^+$ handling

The I_{NaK} model from Winslow et al. (1999) was adjusted to reduce Na$^+$ efflux at fast pacing frequencies (2.5 Hz and above) by reducing dependence on intracellular Na$^+$ concentration (Na$_i$) and increasing voltage dependence of current density (see Appendix). Modified current-voltage relations compare favorably to curves obtained experimentally from guinea pig (human data not available) (Nakao and Gadsby, 1989). I_{NaK} and I_{Nab} current densities were adjusted to achieve a steady-state Na$_i$ of 8 mM at a pacing frequency of 0.25 Hz (see Fig. 5 *B* of Pieske et al., 2002) and to yield changes of steady-state Na$_i$ similar to those measured using SBFI fluorescence at pacing frequencies of 0.5, 1.0, and 2.0 Hz in human left-ventricular myocardium (see Fig. 4 in Pieske et al., 2002). The resulting parameter choices yielded a steady-state value for Na$_i$ of 8 mM at 0.25 Hz, 9.8 mM at 1 Hz, and 13.5 mM at 2 Hz, values that are in the physiological range for Na$_i$ in human myocytes.

Intracellular Ca^{2+} handling

The current model adopts a common pool formulation of intracellular Ca^{2+} cycling similar to that described in Jafri et al. (1998), using continuous-time Markov chain models of sarcolemmal LCCs, RyRs, Ca^{2+} compartmentalization including a model subspace, and realistic intracellular Ca^{2+} buffering.

Numerical methods

For each membrane current, fitting of model transition rates was performed in two steps. First, a cost function defined as the squared error between simulated and experimental responses was minimized globally over the parameter space using a simulated annealing algorithm (Corana, 1987). Second, parameters from the simulated annealing algorithm were selected as initial values for a Neldar-Mead simplex search algorithm (MATLAB), which accepts downhill moves only and has been shown to be superior to the

annealing algorithm if the initial guess is in the vicinity of the global minimum (Corana, 1987; Goffe, 1994). See Appendix for further details.

The whole-cell model is composed of a system of 67 coupled nonlinear differential equations which are integrated numerically to simulate the AP. Numerical integration was performed using the LSODE software package (Hindmarsh, 1983), with 10^{-4} relative error tolerance. The cell model was paced using a stimulus current density of −100 pA/pF and duration of 0.5 ms. The pacing stimulus current was assigned K$^+$ as a charge carrier to eliminate drift of intracellular Na$^+$ and K$^+$ concentrations. This drift has been attributed to neglecting charge contributed by the pacing stimulus during long-term stimulation (Hund et al., 2001). This change allows model ion concentrations to reach a long-term ($\sim10^3$ s) steady state over a broad range of pacing frequencies. Steady-state initial conditions at each pacing frequency are provided in the Appendix. Use of these numerical methods enables simulation of cell electrophysiological responses in real time, despite the high dimensionality of the model.

RESULTS

APs and rate dependence of AP duration

Fig. 5 shows model APs at pacing frequencies of 0.5 Hz (*thick solid line*), 1 Hz (*thin solid line*), and 2 Hz (*dashed line*). Model (Fig. 5) and experimental (see Fig. 1 in Li et al., 1999) frequency dependence of AP shape and duration are in close agreement. Model AP duration to 90% repolarization (APD$_{90}$) decreases monotonically with increasing pacing frequency (407 ms at 0.5 Hz, 322 ms at 1 Hz, and 202 ms at 2 Hz).

Experimental APs vary in shape and duration depending on solutions used, potential ion chelators, overall integrity of the cell after harvesting, precise depth of the cell within the myocardium, and pacing history. Thus, experimentally
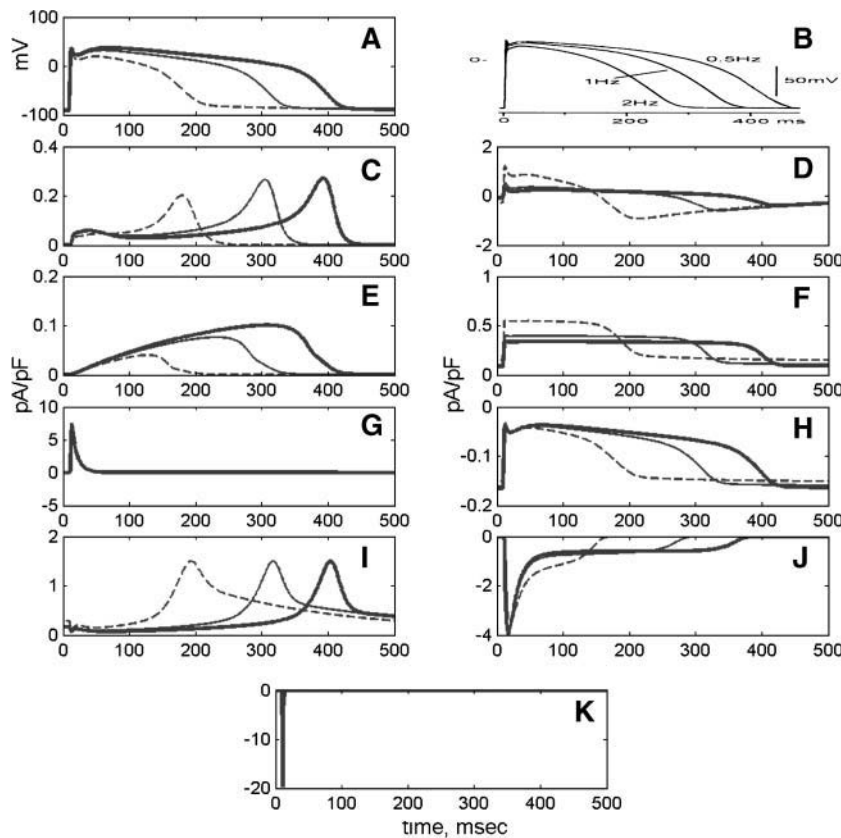
FIGURE 5 AP and major membrane currents at pacing frequencies of 0.5 Hz (*thick solid trace*), 1 Hz (*thin solid trace*), and 2 Hz (*dashed trace*). (*A*) AP. (*B*) Experimental APs from Fig. 1 *A* in Li et al. (1999). (*C*) I_{Kr}; (*D*) I_{NaCa}; (*E*) I_{Ks}; (*F*) I_{NaCa}; (*G*) I_{to1}; (*H*) I_{Nab}; (*I*) I_{K1}; (J) I_{CaL}; and (*K*) I_{Na}.

reported figures for APD in human ventricular myocytes vary substantially. Overall, the model APD at 1 Hz (322 ms) lies in the midrange of experimentally recorded values (336 ± 16 ms, 271 ± 13 ms, and 355 ± 50 ms at 1 Hz pacing frequency; see Li et al., 1999, 1998, 1996).

The contribution of specific membrane currents to rate-dependent adaptation of APD_{90} in human ventricular myocytes remains uncertain (Li et al., 1999). On the basis of experiments and simulation studies in human myocytes and in other species, I_{Ks} (Stengl et al., 2003; Viswanathan et al., 1999); I_{CaL} (Li et al., 1999); I_{to1} (Nabauer et al., 1996); and I_{NaCa} and I_{NaK} (Faber and Rudy, 2000) may be involved. Fig. 5 shows APs and ionic current densities at three pacing frequencies studied after pacing to long-term steady state. APD_{90} decreases from 448 ms at 0.5 Hz to 221 ms at 2 Hz. Corresponding values of Na_i are 8.5 mM and 13.5 mM, respectively. The most obvious increases in outward current density at 2-Hz pacing are Na^+-dependent increases of I_{NaCa} (0.5 pA/pF) and I_{NaK} (0.3 pA/pF) during the initial phase of the AP plateau. These changes contribute to APD shortening at higher pacing frequencies. Fig. 5 also shows that the late component of inward I_{CaL} is increased at 2 Hz. An increase of pacing frequency increases SR Ca^{2+} loading, Ca^{2+} release flux through RyR and thus Ca^{2+}-mediated inactivation of I_{CaL}. However, the reduced plateau potential in response to increased outward I_{NaCa} and I_{NaK} increases the

driving force on Ca^{2+}, leading to a net increase of I_{CaL}. Because of its slow activation properties, the relative contribution of I_{Ks} to repolarization is largest at slower pacing frequencies (the I_{Kr}/I_{Ks} ratio is ~2.5:1 at 0.5 Hz, and is ~5:1 at 2 Hz). However, even at these slower pacing frequencies, its contribution to repolarization remains secondary to that of I_{Kr}. The model suggests that the remaining membrane currents (I_{to1}, I_{K1}, I_{Na}, and I_{Nab}) have little or no role in determining rate-dependence of APD_{90}.

Adaptation of APD_{90} likely occurs as a result of changes in ionic currents due to accumulation of intracellular ions after long-term pacing, as well as short-term changes in current amplitudes due to kinetics of channel gating. The static APD restitution protocol can isolate short-term changes, as intracellular ions do not accumulate significantly over the short extrasystolic interval. In this protocol, after sustained stimulation at a pacing frequency at steady state (S_1 stimuli), a single premature extrasystolic stimulus is delivered at a given diastolic interval, termed an "S_2 stimulus". Extrasystolic APD monotonically increases, rapidly approaching control APD within 200 ms. These data are in qualitative agreement with static restitution curves measured in human left ventricle by Morgan et al. (1992; see also Fig. 6, *A–B*, this article). Examination of membrane currents during the extrasystolic AP (Fig. 6 *C*, *dashed lines*) versus priming control AP (*solid line*) reveals the mechanism for the
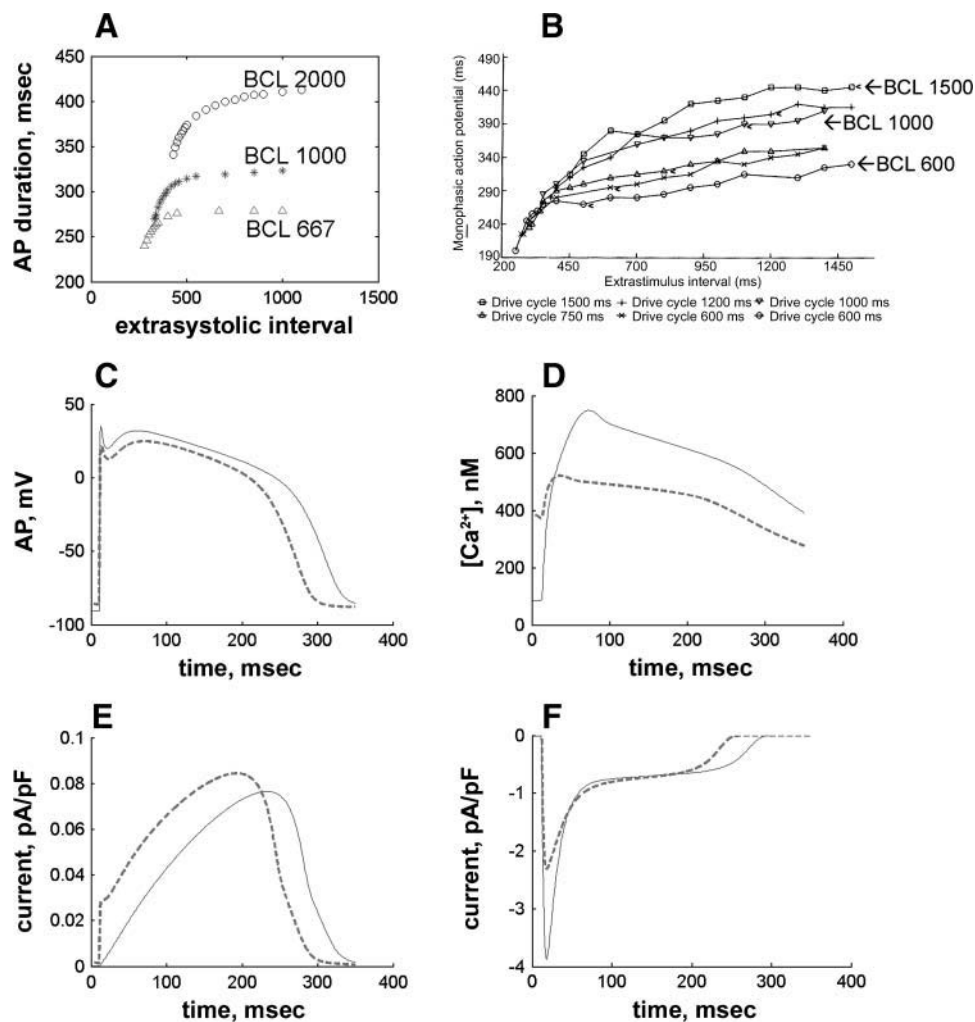
FIGURE 6 Static restitution protocol. (*A*) APD (ordinate, ms) as a function of S_1–S_2 diastolic interval (abscissa, ms) at three different priming frequencies. (*B*) Experimental restitution curves recorded by Morgan et al. (1992). (*C*) APs in response to S_1 (*solid line*) and S_2 (*dashed line*). S_1–S_2 interval for *C–E* set at 350 ms, BCL 1000 ms. (*D*) Intracellular Ca^{2+} transients (ordinate, nM) during the S_1 AP (*solid line*) and the S_2 premature AP (*dashed line*). (*E*) I_{Ks} (ordinate, pA/pF) during the S_1 (*solid line*) and the S_2 APs (*dashed line*). (*F*) I_{CaL} (ordinate, pA/pF) during the S_1 (*solid line*) and S_2 APs (*dashed line*).

short-term changes in APD. The smaller extrasystolic Ca^{2+} transient (Fig. 6 *D*, *dashed line*) induces less calcium-dependent inactivation of I_{CaL}, such that plateau I_{CaL} is slightly higher in the extrasystole (Fig. 6 *F*). However, augmentation of repolarizing I_{Ks} due to incomplete deactivation (Fig. 6 *E*) and early decreases in depolarizing I_{CaL} due to incomplete recovery also contribute to APD shortening.

Ca²⁺ transients

The model is able to predict intracellular Ca^{2+} transients with waveform similar to that observed experimentally. Experimental verification of the steady-state Ca^{2+} transient at 0.25 Hz against the voltage-clamped Ca^{2+} transients recorded by Beuckelmann et al. (1992) is given in Fig. 7, *A–B*. For both model and experiment, a Ca^{2+} transient was elicited with a voltage clamp step to $+10$ mV from a holding potential of -40 mV. Model and experimental Ca^{2+} transients compare well, with similar diastolic and systolic amplitudes (68 nM and 865 nM, respectively, versus

experimental values of 60 nM and 810 nM) and similar time course of activation (time to peak activation 45 ms) and decay (time to half-decay 270 ms for both model and experiment).

Ca²⁺-frequency relations

Experimental studies in nonfailing human myocardium have shown that at physiologic pacing rates (from 0.25 to 3 Hz), intracellular Ca^{2+} levels and twitch force increase monotonically with pacing frequency in a characteristic relation known as the positive Ca^{2+}/force-frequency relation (Maier et al., 2000; Pieske et al., 1995). The model Ca^{2+}-frequency relation was constructed by pacing the cell at frequencies ranging from 0.25 to 3 Hz. Once a long-term steady state was reached at each pacing frequency, peak cytosolic Ca^{2+} was computed. The Ca^{2+} transient amplitude (systolic minus diastolic levels) at each frequency, expressed as percent increase relative to baseline value at 0.25 Hz, is plotted versus pacing frequency in Fig. 7 *C*. Model peak Ca^{2+} levels rise from 438 nM at 0.25 Hz to 1301 nM at 3 Hz—a
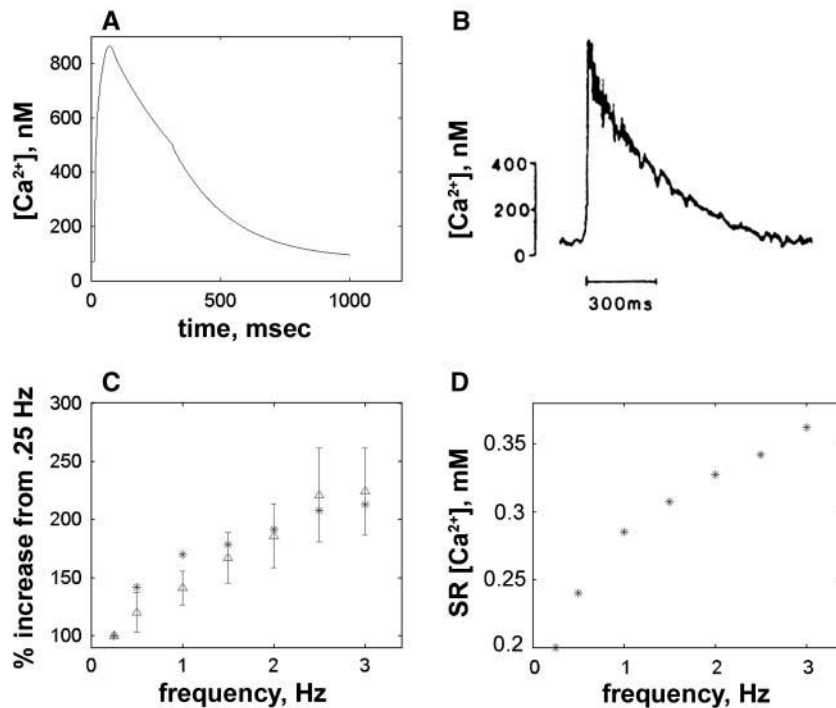
FIGURE 7 Ca^{2+} transient and Ca^{2+}-frequency relation. (*A*) Model Ca^{2+} transient elicited upon voltage clamp to $+10$ mV (ordinate, nM). (*B*) Experimental recording of Ca^{2+} transient elicited upon voltage clamp to $+10$ mV, from Beuckelmann et al. (1992). (*C*) After pacing to long-term steady state at each frequency (abscissa, Hz), percent increase in Ca^{2+} transient amplitude (systolic minus diastolic) from value at 0.25 Hz are plotted for model (ordinate, *asterisks*) and experiment (ordinate, *symbols with error bars*; from Fig. 2 *B* in Maier et al., 2000).

diastolic/peak amplitude increase of 69% at 1 Hz, 91% at 2 Hz, and 113% at 3 Hz. These percent increases are consistent with those measured experimentally in paced human ventricular myocytes, where intracellular Ca^{2+} (systolic minus diastolic) is reported to increase from the 0.25 Hz basal level by $41 \pm 17\%$ at 1 Hz, $86 \pm 26\%$ at 2 Hz, and $124 \pm 36\%$ at 3 Hz (Pieske et al., 1995). The mechanism for the positive Ca^{2+}-frequency relation in the model is twofold: 1), increased loading of JSR Ca^{2+} at higher pacing frequencies leads to larger release events and thus larger intracellular Ca^{2+} transients (see Fig. 7 *D*); and 2), higher Na_i at higher pacing frequencies increase reverse mode I_{NaCa} (see above), leading to greater Ca^{2+} influx during systole.

Extrasystolic restitution and post-extrasystolic potentiation

The model is also able to predict short-term extrasystolic restitution (ESR) and post-extrasystolic potentiation (PESP) relationships measured experimentally. In the ESR/PESP protocol, myocytes are primed at a basal stimulation rate. After steady state has been reached, a premature beat is delivered at a time S_1 after the previous stimulation, where S_1 is less than the basic cycle length. An additional stimulus is then delivered after a fixed post-extrasystolic period S_2. The premature beat is termed the "extrasystole," and the beat that occurs S_2 ms after the extrasystole is termed the "post-

extrasystole." This protocol is repeated for extrasystolic periods of various durations, and twitch force or intracellular calcium is measured for the steady-state beat, the extrasystolic beat, and the post-extrasystolic beat.

Normal human myocardium shows a restitution of the extrasystolic beat—Ca^{2+} transients gradually grow with increasing S_1. The post-extrasystolic beat is potentiated, and produces large calcium transients corresponding to short S_1 and smaller transients corresponding to longer S_1 (Gwathmey et al., 1990). The human myocyte model is able to predict qualitative features of these changes. Fig. 8 contrasts model response with the data of Wier and Yue (1986) recorded in ferret ventricle.

DISCUSSION

A new computational model of the human left-ventricular epicardial myocyte is presented. Models of the voltage-dependent ionic currents I_{Na}, I_{Kr}, I_{Ks}, I_{to1}, I_{K1}, and I_{CaL}, constrained by data obtained from recombinant human channels and/or myocytes isolated from human ventricular epicardium, are shown to accurately reproduce a broad range of experimental data. I_{NaCa} density is constrained using experimental data obtained under conditions where intra- and extracellular Na^+ and Ca^{2+} concentrations and membrane potential are controlled. I_{SERCA} density is constrained using experimental data on Ca^{2+} transient decay
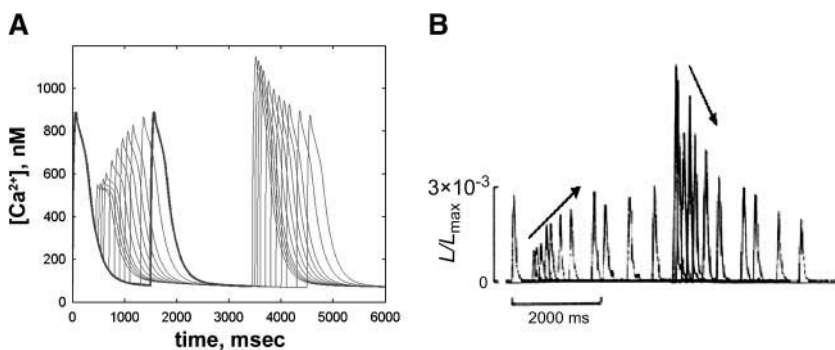
FIGURE 8 Extrasystolic restitution/post-extra-systolic potentiation protocol; see text for details. (A) Model Ca^{2+} transients (ordinate, nM) versus time (abscissa, ms). Thick trace represents beats at priming basic cycle length of 1500 ms. (B) Experiment in ferret ventricle with fluorescence (ordinate, arbitrary units) versus time (abscissa, ms, adapted from Wier and Yue, 1986). L, uncalibrated luminescence signal.

rate under conditions in which I_{NaCa} is either fixed or ablated. I_{NaK} and I_{Nab} densities are constrained using data on the rate of increase of Na_i as a function of pacing frequency.

A critical test of any model is its ability to predict experimental data not included in the fitting process. Experimental data that are predicted as emergent properties of the human myocyte model include: 1), qualitative and quantitative changes of APD_{90} as a function of pacing frequency; 2), quantitative reconstruction of the peak amplitude, time to peak, and half-decay time of the intracellular Ca^{2+} transient at 1-Hz pacing; 3), monotonic increase of the intracellular Ca^{2+} transient peak amplitude as a function of pacing frequency; and 4), qualitative prediction of extrasystolic restitution and post-extrasystolic potentiation responses.

Model results suggest that changes in I_{NaCa} and I_{NaK} produced by changes in Na_i at different pacing frequencies have significant effect on APD_{90}, with factors contributing to increased Na_i producing shortening of the AP. This finding is consistent with recent observations that: 1), increases of Na_i produce substantial shortening of APD_{90} in left-ventricular myocytes isolated from failing human heart through Na^+-induced increases of reverse-mode Na^+-Ca^{2+} exchanger current (Weisser-Thomas et al., 2003); and 2), changing Na_i from 5 to 15 mM decreases APD_{90} of normal canine left-ventricular midmyocardial myocytes from an average of 499.6–327.5 mS through a change in electrical driving force that favors outward current during the early plateau phase of the AP (See Fig. 1 of Armoundas et al., 2003). This finding differs from that of previous simulation studies (Faber and Rudy, 2000; Viswanathan et al., 1999) conducted using models of small mammalian species, which suggest that slow deactivation of I_{Ks} induces channel accumulation in the open state at higher pacing frequencies, thereby leading to APD shortening. One reason may be that unlike in guinea pig, I_{Ks} in canine ventricular myocytes deactivates rapidly, thereby reducing accumulation of I_{Ks} channels in the open state at high pacing frequencies. This, along with the small magnitude of I_{Ks} relative to that of I_{Kr}, may limit the role of I_{Ks} in attenuation of APD at high pacing frequencies in canine and other large mammalian species. However, short-term changes in membrane currents, including I_{Ks} and I_{CaL},

are important in reducing APD in situations where Na_i remains relatively constant, such as in the static restitution protocol. When a single extrasystolic beat is delivered to the model, significant reductions in depolarizing I_{CaL} and a small increase in I_{Ks} is observed. These findings are in agreement with recent experiments by Li et al. (1999), who observed incomplete recovery from inactivation of I_{CaL} at 2 Hz in human ventricular myocytes stimulated by a voltage-clamped action potential waveform.

The model predicts that increased JSR Ca^{2+} load at high pacing frequencies is responsible for the positive Ca^{2+}-frequency relation, a concept well-established experimentally (Maier et al., 2000; Pieske et al., 1999). The increase of JSR Ca^{2+} load is in response to increased Ca^{2+} flux through LCCs (the fraction of time these channels are open is increased at higher pacing frequencies). The model predicts an increase in systolic Ca^{2+} transients even at high pacing rates (>2 Hz), suggesting that in human myocytes, the increase in SR load more than compensates for the negative effects of adaptation of RyR release channels at high stimulation rates. This finding differs from the conclusions of Ten Tusscher et al. (2003) in modeling studies but is consistent with recent recordings of calcium-frequency relations in human ventricle (Maier et al., 2000; Pieske et al., 1995). Model analysis also reveal that increases in reverse-mode I_{NaCa} (brought about by accumulation of Na_i) contribute significantly, but are not necessary to the development of a positive Ca^{2+}-frequency relationship. In simulations in which Na^+ is clamped at a constant value, systolic Ca^{2+} levels still rise with pacing frequency.

Some controversy exists about the role of I_{NaCa} in the ventricular action potential, with some sources indicating that it is entirely or almost entirely an inward current (forward mode) during the action potential (Piacentino et al., 2003; Weber et al., 2002), and others suggesting that it may operate in outward (reverse mode) significantly into the plateau phase (Armoundas et al., 2003; Despa et al., 2002; Pieske et al., 2002; Weisser-Thomas et al., 2003). In the present model, I_{NaCa} is outward for a significant duration of the action potential, suggesting that it plays a role in repolarization and may be important in maintaining SR Ca^{2+} load. To indirectly validate the I_{NaCa} balance, the effects of

exchange inhibitory peptide (XIP, a blocker of I_{NaCa}) were simulated in the model by reducing exchanger density by 50%. Action potential duration is prolonged at intracellular Na$^+$ of 15 mM and to a lesser degree at 10 mM, but is shortened at 5 mM, similar to changes seen experimentally in XIP-loaded canine myocytes (see Fig. 5 B in Armoundas et al., 2003). These data suggest that, in both model and experiment, I_{NaCa} contributes a significant positive repo-larizing current at Na$^+$ of 10 mM or greater (such that inhibition of the current prolongs action potential duration) whereas at low Na$^+$ of 5 mM the current is predominantly inward. The model thus likely correctly represents the balance of outward versus inward I_{NaCa} at physiological Na$_i$ levels.

The model described here has several limitations. First, only qualitative experimental data on the rate-dependence of Na$_i$ concentration are available at present. In addition, the model is overly simplistic in its description of Na$^+$ handling, since significant Na$_i$ gradients may exist due to higher Na$^+$ concentration in a subsarcolemmal "fuzzy space" (Silverman et al., 2003). One recent study by the Bers group (Weber et al., 2003) suggests that the subsarcolemmal Na$^+$ elevation does not significantly augment I_{NaCa} in a rabbit model, lending support to a simpler single-compartment model. However, further experimentation in human myocytes is needed to determine the properties of Na$^+$ handling, as large changes may affect several features of the model, including myocyte repolarization and Ca^{2+} handling secondarily via I_{NaCa}.

A second weakness of the model is that it retains the common-pool formulation of CICR (Stern, 1992). Recent experimental data from both isolated myocytes (Linz and Meyer, 1998; Sipido et al., 1995) as well as recombinant channels expressed in HEK293 cells (Peterson et al., 1999, 2000) show that voltage-dependent inactivation of I_{CaL} is slow and incomplete whereas Ca^{2+}-mediated inactivation is strong, dominating the inactivation process. The opposite is true of existing common pool ventricular myocyte models (see Fig. 10 of Greenstein and Winslow, 2002, and Fig. 5 of Winslow et al., 2001). When Ca^{2+}-dependent inactivation of I_{CaL} is made the dominant inactivation process in common pool models (in which Ca^{2+} release is all or none), I_{CaL} inactivation also exhibits all-or-none behavior. This all or none Ca^{2+}-induced inactivation of I_{CaL} in turn destabilizes the plateau phase of the AP so that APs alternate between those with short (when JSR Ca^{2+} release is regenerative and strongly inactivates I_{CaL}) and long (in the absence of JSR Ca^{2+} release) duration. Thus, common pool models require a dominant voltage-dependent inactivation of I_{CaL} to assure AP stability. A recently developed ventricular myocyte model describing local control of JSR Ca^{2+} release incorporates both the experimentally measured balance between I_{CaL} voltage- and Ca^{2+}-dependent inactivation processes while exhibiting graded JSR Ca^{2+} release, voltage-dependent excitation-contraction coupling gain,

and stable APs (Greenstein and Winslow, 2002). Future work will address the incorporation of the ionic currents described here for the human myocyte model into this local-control model.

Finally, the model presented here does not attempt to reconstruct AP morphology as a function of transmural location. Rather, the focus has been on developing both a reproductive and predictive model of the left-ventricular epicardial myocyte since the majority of experimental data from human ventricular myocytes have been obtained from such cells. Future work will build from this model to address the issue of transmural variation of AP properties.

APPENDIX

Model fitting process

The differential equations describing the time rate of change of the occupancy probabilities of each state in a Markov process can be written (by the law of mass action) as the sum of the transitions entering the current state minus the sum of transitions leaving the state as

$$\frac{dX_i}{dt} = \left(\sum_{j=i}^{N} -a_{ij} \right) X_i + \sum_{j=1}^{N} (a_{ji} X_j), \tag{A1}$$

where X_i is the ith state in the system, a_{ij} is the rate constant for the transition from state i to state j, and N is the number of states in the system.

This can be written in matrix notation as

$$\frac{d\vec{X}}{dt} = A \cdot \vec{X}, \tag{A2}$$

where X is a column vector containing the probability of occupying each state and A is the state transition matrix (A_{ij} being the rate constant for the transition between state i and state j). Under conditions of applied voltage-clamp, A represents a linear time invariant system. The solution of this system is thus a weighted sum of exponentials,

$$\vec{X} = \sum_{i=1}^{N} w_i \cdot \vec{e}_i \cdot \exp(\lambda_i \cdot t), \tag{A3}$$

where λ_i is the ith eigenvalue of the matrix A, e_i is its corresponding eigenvector, and the weights w_i are constants of integration determined by the initial values $X(t = 0)$.

Model fitting was accomplished by minimizing a sum-squared error function, generated by comparing solutions obtained from Eq. A3 to goal data obtained in various voltage-clamp protocols. Data sets utilized for each current are fully described in Methods. Parameters of the model controlling voltage dependence and kinetics of transitions are systematically varied using the simulated annealing algorithm (Corana, 1987). This algorithm randomly searches the parameter space while incrementally decreasing the search radius. Whereas many minimization algorithms accept only downhill moves and tend to converge on local minima, the simulated annealing algorithm accepts uphill moves as well, and thus is more likely to find the global minimum. Uphill moves are accepted based on the Metropolis criterion, a probabilistic function determined from the difference between the new and old errors and the annealing temperature. The annealing temperature controls the rate of convergence by influencing what uphill moves are accepted and by limiting the search radius. To reach a minimum, the annealing temperature is decreased by 5% per 20 N function evaluations, where N is the number of parameters to be determined, as the algorithm converges on a solution. The algorithm is terminated when there is no more than 0.1% change in error since the last temperature reduction.

For fine tuning of the optimal parameter set, the output of the annealing algorithm is fed into a Neldar-Mead simplex search algorithm (in which only downhill moves are accepted). This approach has been shown to be superior in finding the absolute minimum of functions of several variables (Goffe, 1994).

Model equations and parameters

All rate constants are expressed in units of ms^{-1} unless otherwise noted. Similarly, all concentrations are expressed in mM unless otherwise noted.

Constants

See Tables 1–4.

Membrane currents

See Table 5.

Sodium current I_{Na}

$$I_{Na} = \bar{G}_{Na}(O_{1Na} + O_{2Na})(V - E_{Na}). \quad (1)$$

$$E_{Na} = \frac{RT}{F}\ln\left(\frac{[Na^+]_o}{[Na^+]_i}\right). \quad (2)$$

$$\frac{dC_{0Na}}{dt} = -(4\alpha + c_n)(C_{0Na}) + (\beta)(C_{1Na}) + (c_f)(CI_{0Na}). \quad (3)$$

$$\frac{dC_{1Na}}{dt} = -(\beta + c_n \cdot a + 3\alpha)(C_{1Na}) + (4\alpha)(C_{0Na})$$
$$+ (2\beta)(C_{2Na}) + (c_f/a)(CI_{1Na}). \quad (4)$$

$$\frac{dC_{2Na}}{dt} = -(2\beta + c_n \cdot a^2 + 2\alpha)(C_{2Na}) + (3\alpha)(C_{1Na})$$
$$+ (3\beta)(C_{3Na}) + (c_f/a^2)(CI_{2Na}). \quad (5)$$

$$\frac{dC_{3Na}}{dt} = -(3\beta + c_n \cdot a^3 + \alpha)(C_{3Na}) + (2\alpha)(C_{2Na})$$
$$+ (4\beta)(C_{4Na}) + (c_f/a^3)(CI_{3Na}). \quad (6)$$

$$\frac{dC_{4Na}}{dt} = -(4\beta + c_n \cdot a^4 + \gamma + \eta)(C_{4Na})$$
$$+ (\alpha)(C_{3Na}) + (\delta)(O_{1Na}) + (\nu)(O_{2Na})$$
$$+ (c_f/a^4)(CI_{4Na}). \quad (7)$$

$$\frac{dO_{1Na}}{dt} = -(\delta + \varepsilon + o_n)(O_{1Na}) + (\gamma)(C_{4Na})$$
$$+ (\omega)(O_{2Na}) + (o_f)(I_{Na}). \quad (8)$$

TABLE 1 Physical constants

Constant	Symbol	Value
Faraday's constant	F	96.5°C/mmol
Temperature	T	310 K
Gas constant	R	8.315 J/mol −K
Boltzmann's constant	K	1.381 E^{-23} J/K
Planck's constant	H	6.626 E^{-31} J/ms

TABLE 2 Cell geometry constants

Constant	Symbol	Value
Cell capacitance	A_{cap}	153.4 pF
Myoplasm volume	V_{myo}	25.84 E^{-6} μL
Junctional SR volume	V_{JSR}	0.16 E^{-6} μL
Network SR volume	V_{NSR}	2.1 E^{-6} μL
Subspace volume	V_{ss}	1.2 E^{-9} μL

$$\frac{dO_{2Na}}{dt} = -(\omega + \nu)(O_{2Na}) + (\varepsilon)(O_{1Na}) + (\eta)(C_{4Na}). \quad (9)$$

$$\frac{dCI_{0Na}}{dt} = -(c_f + 4\alpha a)(C_{3Na}) + (\beta/a)(CI_{1Na})$$
$$+ (c_n)(C_{0Na}). \quad (10)$$

$$\frac{dCI_{1Na}}{dt} = -(\beta/a + 3\alpha a + c_f/a)(CI_{1Na}) + (4\alpha a)(CI_{0Na})$$
$$+ (2\beta/a)(CI_{2Na}) + (c_n a)(C_{1Na}). \quad (11)$$

$$\frac{dCI_{2Na}}{dt} = -(2\beta/a + 2\alpha a + c_f/a^2)(CI_{2Na}) + (3\alpha a)(CI_{1Na})$$
$$+ (3\beta/a)(CI_{3Na}) + (c_n a^2)(C_{2Na}). \quad (12)$$

$$\frac{dCI_{3Na}}{dt} = -(3\beta/a + \alpha a + c_f/a^3)(CI_{3Na}) + (2\alpha a)(CI_{2Na})$$
$$+ (4\beta/a)(CI_{4Na}) + (c_n a^3)(C_{3Na}). \quad (13)$$

$$\frac{dCI_{4Na}}{dt} = -(4\beta/a + \gamma\gamma + c_f/a^4)(CI_{4Na}) + (\alpha a)(CI_{3Na})$$
$$+ (\delta\delta)(I_{Na}) + (c_n a^4)(C_{4Na}). \quad (14)$$

$$\frac{dI_{Na}}{dt} = -(\delta\delta + o_f)(I_{Na}) + (\gamma\gamma)(CI_{4Na}) + (o_n)(O_{1Na}). \quad (15)$$

See Table 6.

Rapidly-activating delayed rectifier K^+ current I_{Kr}

$$I_{Kr} = \bar{G}_{Kr}f([K^+]_o)(O_{Kr})(V - E_K). \quad (16)$$

$$E_K = \frac{RT}{F}\ln\left(\frac{[K^+]_o}{[K^+]_i}\right). \quad (17)$$

$$f([K^+]_o) = \sqrt{\left(\frac{[K^+]_o}{4}\right)}. \quad (18)$$

$$\frac{dC_{1Kr}}{dt} = -(\alpha_0)(C_{1Kr}) + (\beta_0)(C_{2Kr}). \quad (19)$$

$$\frac{dC_{2Kr}}{dt} = -(\beta_0 + k_f)(C_{2Kr}) + (\alpha_0)(C_{1Kr}) + (k_b)(C_{3Kr}). \quad (20)$$

TABLE 3 Standard ionic concentrations

Permeant ion	Symbol	Value
Sodium	$[Na^+]_o$	138 mM
Potassium	$[K^+]_o$	4 mM
Calcium	$[Ca^{2+}]_o$	2 mM

TABLE 4   Initial conditions (pacing protocol)

State	Symbol	0.25 Hz	1 Hz	2 Hz	3 Hz
Membrane potential, mV	V	$-9.121\,E^{+01}$	$-9.066\,E^{+01}$	$-8.877\,E^{+01}$	$-8.615\,E^{+01}$
Intracellular sodium, mM	$[\text{Na}^+]_i$	$8.006\,E^{+00}$	$9.798\,E^{+00}$	$1.347\,E^{+01}$	$1.649\,E^{+01}$
Intracellular potassium, mM	$[\text{K}^+]_i$	$1.274\,E^{+02}$	$1.256\,E^{+02}$	$1.219\,E^{+02}$	$1.188\,E^{+02}$
Intracellular calcium, mM	$[\text{Ca}^{2+}]_i$	$4.414\,E^{-05}$	$8.601\,E^{-05}$	$2.447\,E^{-04}$	$4.781\,E^{-04}$
NSR calcium, mM	$[\text{Ca}^{2+}]_{\text{NSR}}$	$1.741\,E^{-01}$	$2.855\,E^{-01}$	$3.260\,E^{-01}$	$3.689\,E^{-01}$
SS calcium, mM	$[\text{Ca}^{2+}]_{\text{SS}}$	$4.803\,E^{-05}$	$1.420\,E^{-04}$	$3.386\,E^{-04}$	$6.320\,E^{-04}$
JSR calcium, mM	$[\text{Ca}^{2+}]_{\text{JSR}}$	$1.741\,E^{-01}$	$2.852\,E^{-01}$	$3.242\,E^{-01}$	$3.662\,E^{-01}$
RyR state C_1	P_{C1}	$9.366\,E^{-01}$	$4.448\,E^{-01}$	$2.207\,E^{-01}$	$1.345\,E^{-01}$
RyR state O_1	P_{O1}	$7.516\,E^{-05}$	$6.602\,E^{-04}$	$9.747\,E^{-04}$	$1.414\,E^{-03}$
RyR state C_2	P_{C2}	$6.337\,E^{-02}$	$5.545\,E^{-01}$	$7.783\,E^{-01}$	$8.641\,E^{-01}$
RyR state O_2	P_{O2}	$1.749\,E^{-11}$	$3.974\,E^{-09}$	$7.976\,E^{-08}$	$7.544\,E^{-07}$
L-type state C_0	$C_{0\text{L}}$	$9.861\,E^{-01}$	$8.622\,E^{-01}$	$6.745\,E^{-01}$	$6.122\,E^{-01}$
L-type state C_1	$C_{1\text{L}}$	$1.251\,E^{-02}$	$1.141\,E^{-02}$	$1.033\,E^{-02}$	$1.146\,E^{-02}$
L-type state C_2	$C_{2\text{L}}$	$5.955\,E^{-05}$	$5.666\,E^{-05}$	$5.933\,E^{-05}$	$8.050\,E^{-05}$
L-type state C_3	$C_{3\text{L}}$	$1.260\,E^{-07}$	$1.250\,E^{-07}$	$1.514\,E^{-07}$	$2.512\,E^{-07}$
L-type state C_4	$C_{4\text{L}}$	$9.990\,E^{-11}$	$1.034\,E^{-10}$	$1.450\,E^{-10}$	$2.940\,E^{-10}$
L-type state O	O_{L}	$7.493\,E^{-12}$	$7.758\,E^{-12}$	$1.088\,E^{-11}$	$2.209\,E^{-11}$
L-type state C_{ca0}	C_{Ca0L}	$1.210\,E^{-03}$	$1.199\,E^{-01}$	$2.965\,E^{-01}$	$3.493\,E^{-01}$
L-type state C_{ca1}	C_{Ca1L}	$6.140\,E^{-05}$	$6.347\,E^{-03}$	$1.816\,E^{-02}$	$2.616\,E^{-02}$
L-type state C_{ca2}	C_{Ca2L}	$1.169\,E^{-06}$	$1.260\,E^{-04}$	$4.172\,E^{-04}$	$7.349\,E^{-04}$
L-type state C_{ca3}	C_{Ca3L}	$9.889\,E^{-09}$	$1.112\,E^{-06}$	$4.260\,E^{-06}$	$9.175\,E^{-06}$
L-type state C_{ca4}	C_{Ca4L}	$3.137\,E^{-11}$	$3.681\,E^{-09}$	$1.631\,E^{-08}$	$4.295\,E^{-08}$
L-type inactivation variable	y	$9.997\,E^{-01}$	$9.997\,E^{-01}$	$9.996\,E^{-01}$	$9.993\,E^{-01}$
High affinity troponin bound fraction	$HTRPN_{\text{Ca}}$	$9.359\,E^{-01}$	$9.772\,E^{-01}$	$9.912\,E^{-01}$	$9.948\,E^{-01}$
Low affinity troponin bound fraction	$LTRPN_{\text{Ca}}$	$4.233\,E^{-02}$	$8.047\,E^{-02}$	$2.070\,E^{-01}$	$3.374\,E^{-01}$
Kv4.3 state C_1	$C_{1\text{Kvf}}$	$9.527\,E^{-01}$	$9.514\,E^{-01}$	$9.460\,E^{-01}$	$9.335\,E^{-01}$
Kv4.3 state C_2	$C_{2\text{Kvf}}$	$2.563\,E^{-02}$	$2.668\,E^{-02}$	$3.063\,E^{-02}$	$3.685\,E^{-02}$
Kv4.3 state C_3	$C_{3\text{Kvf}}$	$2.586\,E^{-04}$	$2.806\,E^{-04}$	$3.719\,E^{-04}$	$5.457\,E^{-04}$
Kv4.3 state C_4	$C_{4\text{Kvf}}$	$1.159\,E^{-06}$	$1.312\,E^{-06}$	$2.007\,E^{-06}$	$3.597\,E^{-06}$
Kv4.3 state O	O_{Kvf}	$1.949\,E^{-09}$	$2.300\,E^{-09}$	$4.062\,E^{-09}$	$8.887\,E^{-09}$
Kv4.3 state CI_1	$CI_{1\text{Kvf}}$	$1.514\,E^{-02}$	$1.513\,E^{-02}$	$1.523\,E^{-02}$	$1.755\,E^{-02}$
Kv4.3 state CI_2	$CI_{2\text{Kvf}}$	$5.225\,E^{-03}$	$5.443\,E^{-03}$	$6.326\,E^{-03}$	$8.912\,E^{-03}$
Kv4.3 state CI_3	$CI_{3\text{Kvf}}$	$9.131\,E^{-04}$	$9.918\,E^{-04}$	$1.332\,E^{-03}$	$2.302\,E^{-03}$
Kv4.3 state CI_4	$CI_{4\text{Kvf}}$	$8.401\,E^{-05}$	$9.514\,E^{-05}$	$1.478\,E^{-04}$	$3.132\,E^{-04}$
Kv4.3 state I	$OI_{1\text{Kvf}}$	$2.323\,E^{-06}$	$2.743\,E^{-06}$	$4.918\,E^{-06}$	$1.271\,E^{-05}$
Kv1.4 state C_1	$C_{1\text{Kvs}}$	$7.630\,E^{-01}$	$5.977\,E^{-01}$	$3.411\,E^{-01}$	$2.189\,E^{-01}$
Kv1.4 state C_2	$C_{2\text{Kvs}}$	$2.108\,E^{-01}$	$1.731\,E^{-01}$	$1.162\,E^{-01}$	$9.330\,E^{-02}$
Kv1.4 state C_3	$C_{3\text{Kvs}}$	$2.184\,E^{-02}$	$1.881\,E^{-02}$	$1.488\,E^{-02}$	$1.497\,E^{-02}$
Kv1.4 state C_4	$C_{4\text{Kvs}}$	$1.006\,E^{-03}$	$9.161\,E^{-04}$	$8.710\,E^{-04}$	$1.105\,E^{-03}$
Kv1.4 state O	O_{Kvs}	$1.737\,E^{-05}$	$1.976\,E^{-05}$	$2.946\,E^{-05}$	$4.912\,E^{-05}$
Kv1.4 state CI_1	$CI_{1\text{Kvs}}$	$6.505\,E^{-04}$	$3.539\,E^{-02}$	$5.392\,E^{-02}$	$3.209\,E^{-02}$
Kv1.4 state CI_2	$CI_{2\text{Kvs}}$	$9.517\,E^{-05}$	$5.429\,E^{-03}$	$9.733\,E^{-03}$	$7.252\,E^{-03}$
Kv1.4 state CI_3	$CI_{3\text{Kvs}}$	$3.820\,E^{-04}$	$2.288\,E^{-02}$	$4.847\,E^{-02}$	$4.543\,E^{-02}$
Kv1.4 state CI_4	$CI_{4\text{Kvs}}$	$5.143\,E^{-04}$	$3.234\,E^{-02}$	$8.089\,E^{-02}$	$9.521\,E^{-02}$
Kv1.4 state I	$OI_{1\text{Kvs}}$	$1.719\,E^{-03}$	$1.134\,E^{-01}$	$3.339\,E^{-01}$	$4.917\,E^{-01}$
I_{Kr} state C_1	$C_{1\text{Kr}}$	$9.967\,E^{-01}$	$9.967\,E^{-01}$	$9.966\,E^{-01}$	$9.965\,E^{-01}$
I_{Kr} state C_2	$C_{2\text{Kr}}$	$4.163\,E^{-04}$	$4.341\,E^{-04}$	$5.013\,E^{-04}$	$6.116\,E^{-04}$
I_{Kr} state C_3	$C_{3\text{Kr}}$	$7.321\,E^{-05}$	$7.634\,E^{-05}$	$8.827\,E^{-05}$	$1.089\,E^{-04}$
I_{Kr} state O	O_{Kr}	$8.847\,E^{-06}$	$9.512\,E^{-06}$	$1.242\,E^{-05}$	$2.827\,E^{-05}$
I_{Kr} state I	I_{Kr}	$1.387\,E^{-06}$	$1.533\,E^{-06}$	$2.207\,E^{-06}$	$5.805\,E^{-06}$
I_{Ks} state C_0	$C_{0\text{Ks}}$	$9.646\,E^{-01}$	$9.646\,E^{-01}$	$9.634\,E^{-01}$	$9.626\,E^{-01}$
I_{Ks} state C_1	$C_{1\text{Ks}}$	$3.543\,E^{-02}$	$3.543\,E^{-02}$	$3.546\,E^{-02}$	$3.547\,E^{-02}$
I_{Ks} state O_1	$O_{1\text{Ks}}$	$2.294\,E^{-07}$	$2.492\,E^{-07}$	$3.349\,E^{-07}$	$4.987\,E^{-07}$
I_{Ks} state O_2	$O_{2\text{Ks}}$	$4.680\,E^{-11}$	$1.299\,E^{-05}$	$1.164\,E^{-03}$	$1.894\,E^{-03}$
I_{Na} state C_0	$C_{0\text{Na}}$	$1.474\,E^{-01}$	$1.438\,E^{-01}$	$1.305\,E^{-01}$	$1.094\,E^{-01}$
I_{Na} state C_1	$C_{1\text{Na}}$	$4.051\,E^{-02}$	$4.178\,E^{-02}$	$4.597\,E^{-02}$	$5.020\,E^{-02}$
I_{Na} state C_2	$C_{2\text{Na}}$	$4.175\,E^{-03}$	$4.553\,E^{-03}$	$6.069\,E^{-03}$	$8.639\,E^{-03}$
I_{Na} state C_3	$C_{3\text{Na}}$	$1.913\,E^{-04}$	$2.205\,E^{-04}$	$3.562\,E^{-04}$	$6.607\,E^{-04}$
I_{Na} state C_4	$C_{4\text{Na}}$	$3.286\,E^{-06}$	$4.005\,E^{-06}$	$7.838\,E^{-06}$	$1.895\,E^{-05}$
I_{Na} state O_1	$O_{1\text{Na}}$	$1.196\,E^{-08}$	$1.574\,E^{-08}$	$4.002\,E^{-08}$	$1.378\,E^{-07}$
I_{Na} state O_2	$O_{2\text{Na}}$	$2.160\,E^{-09}$	$2.857\,E^{-09}$	$7.408\,E^{-09}$	$2.636\,E^{-08}$
I_{Na} state CI_0	$CI_{0\text{Na}}$	$4.869\,E^{-01}$	$4.750\,E^{-01}$	$4.314\,E^{-01}$	$3.619\,E^{-01}$

TABLE 4 Continued

State	Symbol	0.25 Hz	1 Hz	2 Hz	3 Hz
I_{Na} state CI_1	CI_{1Na}	$2.625\ E^{-01}$	$2.707\ E^{-01}$	$2.979\ E^{-01}$	$3.257\ E^{-01}$
I_{Na} state CI_2	CI_{2Na}	$5.306\ E^{-02}$	$5.786\ E^{-02}$	$7.715\ E^{-02}$	$1.099\ E^{-01}$
I_{Na} state CI_3	CI_{3Na}	$4.768\ E^{-03}$	$5.496\ E^{-03}$	$8.880\ E^{-03}$	$1.649\ E^{-02}$
I_{Na} state CI_4	CI_{4Na}	$1.606\ E^{-04}$	$1.958\ E^{-04}$	$3.833\ E^{-04}$	$9.297\ E^{-04}$
I_{Na} state I	I_{Na}	$3.097\ E^{-04}$	$4.177\ E^{-04}$	$1.271\ E^{-03}$	$1.605\ E^{-02}$

$$\frac{dO_{Kr}}{dt} = -(\beta_1 + \alpha_i)(O_{Kr}) + (\alpha_1)(C_{3Kr}) + (\beta_i)(I_{Kr}). \quad (21)$$

$$\frac{dO_{Kr}}{dt} = -(\beta_1 + \alpha_i)(O_{Kr}) + (\alpha_1)(C_{3Kr}) + (\beta_i)(I_{Kr}). \quad (22)$$

$$\frac{dI_{Kr}}{dt} = -(\psi + \beta_i)(I_{Kr}) + (\alpha_{i3})(C_{3Kr}) + (\alpha_i)(O_{Kr}). \quad (23)$$

$$\psi = \frac{(\beta_1 \cdot \beta_i \cdot \alpha_{i3})}{(\alpha_1 \cdot \alpha_i)}. \quad (24)$$

See Table 7.

Slowly-activating delayed rectifier K^+ current I_{Ks}

$$I_{Ks} = \bar{G}_{Ks}(O_{1Ks} + O_{2Ks})(V - E_K). \quad (25)$$

$$E_K = \frac{RT}{F}\ln\left(\frac{[K^+]_o}{[K^+]_i}\right). \quad (26)$$

$$\frac{dC_{0Ks}}{dt} = -(\alpha)(C_{0Ks}) + (\beta)(C_{1Ks}). \quad (27)$$

$$\frac{dC_{1Ks}}{dt} = -(\beta + \gamma)(C_{1Ks}) + (\alpha)(C_{0Ks}) + (\delta)(O_{1Ks}). \quad (28)$$

$$\frac{dO_{1Ks}}{dt} = -(\delta + \varepsilon)(O_{1Ks}) + (\gamma)(C_{1Ks}) + (\omega)(O_{2Ks}). \quad (29)$$

$$\frac{dO_{2Ks}}{dt} = -(\omega)(O_{2Ks}) + (\varepsilon)(O_{1Ks}). \quad (30)$$

See Table 8.

Transient outward K^+ current I_{to1}

Fast recovering component, $Kv4.3$

$$I_{Kv4.3} = \bar{G}_{Kv4.3}(O_{Kvf})(V - E_K). \quad (31)$$

$$E_K = \frac{RT}{F}\ln\left(\frac{[K^+]_o}{[K^+]_i}\right). \quad (32)$$

TABLE 5 Time-dependent current densities

Current	Symbol	Density
Sodium current	G_{Na}	56.32 mS/μF
Delayed rectifier, rapid component	G_{Kr}	0.0186 mS/μF
Delayed rectifier, slow component	G_{Ks}	0.0035 mS/μF
Transient outward current, fast recovery	$G_{Kv4.3}$	0.0775 mS/μF
Transient outward current, slow recovery	$P_{Kv1.4}$	$4.161\ d^{-8}$ cm/s

$$\frac{dC_{0Kvf}}{dt} = -(4\alpha_a + \beta_i)(C_{0Kvf}) + (\beta_a)(C_{1Kvf}) + (\alpha_i)(CI_{0Kvf}). \quad (33)$$

$$\frac{dC_{1Kvf}}{dt} = -(\beta_a + 3\alpha_a + f_1\beta_i)(C_{1Kvf}) + (4\alpha_a)(C_{0Kvf}) + (2\beta_a)(C_{2Kvf}) + (\alpha_i/b_1)(CI_{1Kvf}). \quad (34)$$

$$\frac{dC_{2Kvf}}{dt} = -(2\beta_a + 2\alpha_a + f_2\beta_i)(C_{2Kvf}) + (3\alpha_a)(C_{1Kvf}) + (3\beta_a)(C_{3Kvf}) + (\alpha_i/b_2)(CI_{2Kvf}). \quad (35)$$

$$\frac{dC_{3Kvf}}{dt} = -(3\beta_a + \alpha_a + f_3\beta_i)(C_{3Kvf}) + (2\alpha_a)(C_{2Kvf}) + (4\beta_a)(C_{4Kvf}) + (\alpha_i/b_3)(CI_{3Kvf}). \quad (36)$$

$$\frac{dO_{Kvf}}{dt} = -(4\beta_a + f_4\beta_i)(O_{Kvf}) + (\alpha_a)(C_{3Kvf}) + (\alpha_i/b_4)(OI_{Kvf}). \quad (37)$$

$$\frac{dCI_{0Kvf}}{dt} = -(b_1 4\alpha_a + a_i)(CI_{0Kvf}) + (\beta_a/f_1)(CI_{1Kvf}) + (\beta_i)(C_{0Kvf}). \quad (38)$$

TABLE 6 I_{Na} rate constants

	$\lambda = Q\dfrac{kT}{h}\exp\left(\dfrac{-\Delta H_\lambda}{RT} + \dfrac{\Delta S_\lambda}{R} + \dfrac{z_\lambda FV}{RT}\right)$ parameters		
Rate constant	ΔH, J/mol	ΔS, J/mol $-$K	z
α	114,007	224.114	0.2864
β	272,470	708.146	-2.2853
γ	196,337	529.952	2.7808
δ	133,690	229.205	-1.5580
O_n	62,123	39.295	0.2888
O_f	97,658	1.510	0.0685
$\gamma\gamma$	$-116,431$	-578.317	0.7641
$\delta\delta$	55,701	-130.639	-3.6498
ε	85,800	70.078	0
ω	121,955	225.175	0
η	147,814	338.915	2.1360
ν	121,322	193.265	-1.7429
C_n	287,913	786.217	0
C_f	59,565	0.00711	0
Scaling a	1.4004		
Q	1.389		

TABLE 7 I_{Kr} **rate constants**

Rate constant	Value
α_o	$0.0171 \cdot \exp(0.0330\ V)\ \text{ms}^{-1}$
β_o	$0.0397 \cdot \exp(-0.0431\ V)\ \text{ms}^{-1}$
α_1	$0.0206 \cdot \exp(0.0262\ V)\ \text{ms}^{-1}$
β_1	$0.0013 \cdot \exp(-0.0269\ V)\ \text{ms}^{-1}$
α_i	$0.1067 \cdot \exp(0.0057\ V)\ \text{ms}^{-1}$
β_i	$0.0065 \cdot \exp(-0.0454\ V)\ \text{ms}^{-1}$
α_{i3}	$8.04\ E^{-5} \cdot \exp(6.98\ E^{-7}\ V)\ \text{ms}^{-1}$
k_f	$0.0261\ \text{ms}^{-1}$
k_b	$0.1483\ \text{ms}^{-1}$

$$\frac{dCI_{1Kvf}}{dt} = -(\beta_a/f_1 + b_3 3\alpha_a/b_1 + \alpha_i/b_1)(CI_{1Kvf})$$
$$+ (b_1 4\alpha_a)(CI_{0Kvf}) + (f_1 2\beta_a/f_2)(CI_{2Kvf})$$
$$+ (f_1\beta_i)(C_{1Kvf}). \tag{39}$$

$$\frac{dCI_{2Kvf}}{dt} = -(f_1 2\beta_a/f_2 + b_3 2\alpha_a/b_2 + \alpha_i/b_2)(CI_{2Kvf})$$
$$+ (b_2 3\alpha_a/b_1)(CI_{1Kvf}) + (f_2 3\beta_a/f_3)(CI_{3Kvf})$$
$$+ (f_2\beta_i)(C_{2Kvf}). \tag{40}$$

$$\frac{dCI_{3Kvf}}{dt} = -(f_2 3\beta_a/f_3 + b_4\alpha_a/b_3 + \alpha_i/b_3)(CI_{3Kvf})$$
$$+ (b_3 2\alpha_a/b_2)(CI_{2Kvf}) + (f_3 4\beta_a/f_4)(OI_{Kvf})$$
$$+ (f_3\beta_i)(C_{3Kvf}). \tag{41}$$

$$\frac{dOI_{Kvf}}{dt} = -(f_3 4\beta_a/f_4 + \alpha_i/b_4)(OI_{Kvf}) + (b_4\alpha_a/b_3)$$
$$\times (CI_{3Kvf}) + (f_4\beta_i)(O_{Kvf}). \tag{42}$$

Slowly recovering component, Kv1.4

$$I_{Kv1.4} = P_{Kv1.4}O_{Kvs}\frac{4VF^2}{RT}\frac{[\text{K}^+]_i\exp\left(\frac{VF}{RT}\right) - [\text{K}^+]_o}{\exp\left(\frac{VF}{RT}\right) - 1} + I_{Kv1.4,Na}. \tag{43}$$

$$I_{Kv1.4,Na} = 0.02 \cdot P_{Kv1.4}O_{Kvs}\frac{4VF^2}{RT}\frac{[\text{Na}^+]_i\exp\left(\frac{VF}{RT}\right) - [\text{Na}^+]_o}{\exp\left(\frac{VF}{RT}\right) - 1}. \tag{44}$$

TABLE 8 I_{Ks} **rate constants**

Rate constant	Value
α	$7.956\ E^{-3}\ \text{ms}^{-1}$
β	$2.16\ E^{-1} \cdot \exp(-0.00002\ V)\ \text{ms}^{-1}$
γ	$3.97\ E^{-2}\ \text{ms}^{-1}$
δ	$7\ E^{-3} \cdot \exp(-0.15\ V)\ \text{ms}^{-1}$
ε	$7.67\ E^{-3} \cdot \exp(0.087\ V)\ \text{ms}^{-1}$
ω	$3.80\ E^{-3} \cdot \exp(-0.014\ V)\ \text{ms}^{-1}$

$$\frac{dC_{0Kvs}}{dt} = -(4\alpha_a + \beta_i)(C_{0Kvs}) + (\beta_a)(C_{1Kvs})$$
$$+ (\alpha_i)(CI_{0Kvs}). \tag{45}$$

$$\frac{dC_{1Kvs}}{dt} = -(\beta_a + 3\alpha_a + f_1\beta_i)(C_{1Kvs}) + (4\alpha_a)(C_{0Kvs})$$
$$+ (2\beta_a)(C_{2Kvs}) + (\alpha_i/b_1)(CI_{1Kvs}). \tag{46}$$

$$\frac{dC_{2Kvs}}{dt} = -(2\beta_a + 2\alpha_a + f_2\beta_i)(C_{2Kvs})$$
$$+ (3\alpha_a)(C_{1Kvs}) + (3\beta_a)(C_{3Kvs}) + (\alpha_i/b_2)(CI_{2Kvs}). \tag{47}$$

$$\frac{dC_{3Kvs}}{dt} = -(3\beta_a + \alpha_a + f_3\beta_i)(C_{3Kvs}) + (2\alpha_a)(C_{2Kvs})$$
$$+ (4\beta_a)(C_{4Kvs}) + (\alpha_i/b_3)(CI_{3Kvs}). \tag{48}$$

$$\frac{dO_{Kvs}}{dt} = -(4\beta_a + f_4\beta_i)(O_{Kvs}) + (\alpha_a)(C_{3Kvs})$$
$$+ (\alpha_i/b_4)(OI_{Kvs}). \tag{49}$$

$$\frac{dCI_{0Kvs}}{dt} = -(b_1 4\alpha_a + a_i)(CI_{0Kvs}) + (\beta_a/f_1)(CI_{1Kvs})$$
$$+ (\beta_i)(C_{0Kvs}). \tag{50}$$

$$\frac{dCI_{1Kvs}}{dt} = -(\beta_a/f_1 + b_2 3\alpha_a/b_1 + \alpha_i/b_1)(CI_{1Kvs})$$
$$+ (b_1 4\alpha_a)(CI_{0Kvs}) + (f_1 2\beta_a/f_2)(CI_{2Kvs})$$
$$+ (f_1\beta_i)(C_{1Kvs}). \tag{51}$$

$$\frac{dCI_{2Kvs}}{dt} = -(f_1 2\beta_a/f_2 + b_3 2\alpha_a/b_2 + \alpha_i/b_2)(CI_{2Kvs})$$
$$+ (b_2 3\alpha_a/b_1)(CI_{1Kvs}) + (f_2 3\beta_a/f_3)(CI_{3Kvs})$$
$$+ (f_2\beta_i)(C_{2Kvs}). \tag{52}$$

$$\frac{dCI_{3Kvs}}{dt} = -(f_2 3\beta_a/f_3 + b_4\alpha_a/b_3 + \alpha_i/b_3)(CI_{3Kvs})$$
$$+ (b_3 2\alpha_a/b_2)(CI_{2Kvs}) + (f_3 4\beta_a/f_4)(OI_{Kvs})$$
$$+ (f_3\beta_i)(C_{3Kvs}). \tag{53}$$

$$\frac{dOI_{Kvs}}{dt} = -(f_3 4\beta_a/f_4 + \alpha_i/b_4)(OI_{Kvs}) + (b_4\alpha_a/b_3)(CI_{3Kvs})$$
$$+ (f_4\beta_i)(O_{Kvs}). \tag{54}$$

See Table 9.

Time-independent K$^+$ current I_{K1}

$$I_{K1} = \bar{G}_{K1}K_1^\infty(V)\left(\sqrt{[\text{K}^+]_o}\right)(V - E_K). \tag{55}$$

TABLE 9 I_{to1} **rate constants**

Rate constant	$Kv4.3$ current, ms^{-1}	$Kv1.4$ current, ms^{-1}
α_a	$0.675{,}425 \cdot \exp(0.0255\,V)$	$1.840024 \cdot \exp(0.0077\,V)$
β_a	$0.088269 \cdot \exp(-0.0883\,V)$	$0.010817 \cdot \exp(-0.0779\,V)$
α_i	0.109566	0.003058
β_i	$3.03334\,E^{-4}$	$2.4936\,E^{-6}$
f_1	1.66120	0.52465
f_2	22.2463	17.5188
f_3	195.978	938.587
f_4	181.609	54749.1
b_1	0.72246	1.00947
b_2	0.47656	1.17100
b_3	7.77537	0.63902
b_4	318.232	2.12035

$$K_1^\infty(V) = \frac{1}{0.94 + \exp\left(\dfrac{1.26}{RT/F}(V - EK)\right)}. \tag{56}$$

$$E_K = \frac{RT}{F}\ln\left(\frac{[K^+]_o}{[K^+]_i}\right). \tag{57}$$

$$\bar{G}_{K1} = 0.125\frac{mS}{\mu F \cdot mM^{1/2}}. \tag{58}$$

Sodium handling mechanisms

NCX current I_{NaCa}

$$I_{NaCa} = k_{NaCa}\frac{1}{K_{m,Na}^3 + [Na^+]_o^3}\frac{1}{K_{m,Ca} + [Ca^{2+}]_o}\frac{1}{1 + k_{sat}e^{(\eta-1)\frac{VF}{RT}}}$$
$$\times \left(e^{\frac{\eta VF}{RT}}[Na^+]_i^3[Ca^{2+}]_o - e^{\frac{(\eta-1)VF}{RT}}[Na^+]_o^3[Ca^{2+}]_i\right). \tag{59}$$

Na^+ background current $I_{Na,b}$

$$I_{Na,b} = \bar{G}_{Na,b}(V - E_{Na}). \tag{60}$$

Na^+-K^+ pump current I_{NaK}

$$I_{NaK} = k_{NaK}f_{NaK}\frac{1}{1 + \left(\frac{K_{m,Nai}}{[Na^+]_i}\right)^{1.5}}\frac{[K^+]_o}{[K^+]_o + K_{m,Ko}}. \tag{61}$$

$$f_{NaK} = \frac{1}{1 + 0.1245e^{-0.1\frac{VF}{RT}} + 0.0365\sigma e^{-1.33\frac{VF}{RT}}}. \tag{62}$$

$$\sigma = \frac{1}{7}\left(e^{\frac{[Na^+]_o}{67.3}} - 1\right). \tag{63}$$

See Table 10.

TABLE 10 **Sodium handling parameters**

Parameter	Value
$G_{Na,b}$	0.001 mS/μF
$K_{m,Na}$	87.5 mM
$K_{m,Ca}$	1.38 mM
k_{sat}	0.2
η	0.35
k_{NaK}	2.387 μA/μF
$K_{m,Nai}$	20 mM
$K_{m,Ko}$	1.5 mM

Calcium handling mechanisms

Sarcolemmal Ca^{2+} pump current $I_{p(Ca)}$

$$I_{p(Ca)} = \bar{I}_{p(Ca)}\frac{[Ca^{2+}]_i}{K_{m,p(Ca)} + [Ca^{2+}]_i}. \tag{64}$$

Ca^{2+} background current $I_{Ca,b}$

$$I_{Ca,b} = \bar{G}_{Ca,b}(V - E_{Ca}). \tag{65}$$

$$E_{Ca} = \frac{RT}{2F}\ln\left(\frac{[Ca^{2+}]_o}{[Ca^{2+}]_i}\right). \tag{66}$$

See Table 11.

L-type Ca^{2+} current I_{Ca}

$$\alpha = 1.997e^{0.012(V-35)}. \tag{67}$$

$$\beta = 0.0882e^{-0.065(V-22)}. \tag{68}$$

$$\alpha' = \alpha a. \tag{69}$$

$$\beta' = \frac{\beta}{b}. \tag{70}$$

$$\gamma = 0.0554[Ca^{2+}]_{ss}. \tag{71}$$

$$\frac{dC_{0L}}{dt} = -(4\alpha + \gamma)C_{0L} + \beta C_{1L} + \omega C_{Ca0L}. \tag{72}$$

$$\frac{dC_{1L}}{dt} = -(3\alpha + \beta + \gamma a)C_{1L} + 4\alpha C_{0L} + 2\beta C_{2L} + \frac{\omega}{b}C_{Ca1L}. \tag{73}$$

$$\frac{dC_{2L}}{dt} = -(2\alpha + 2\beta + \gamma a^2)C_{2L} + 3\alpha C_{1L} + 3\beta C_{3L} + \frac{\omega}{b^2}C_{Ca2L}. \tag{74}$$

$$\frac{dC_{3L}}{dt} = -(\alpha + 3\beta + \gamma a^3)C_{3L} + 2\alpha C_{2L} + 4\beta C_{4L} + \frac{\omega}{b^3}C_{Ca3L}. \tag{75}$$

$$\frac{dC_{4L}}{dt} = -(f + 4\beta + \gamma a^4)C_{4L} + \alpha C_{3L} + gO_L + \frac{\omega}{b^4}C_{Ca4L}. \tag{76}$$

TABLE 11 Membrane calcium exchangers, background current

Parameter	Value
$\bar{I}_{\text{p(Ca)}}$	0.05 pA/pF
$K_{\text{m,p(Ca)}}$	0.0005 mM
$\bar{G}_{\text{Ca,b}}$	7.684 d^{-5} ms/μF

$$\frac{dO_L}{dt} = -gO_L + fC_{4L}. \tag{77}$$

$$\frac{dC_{\text{Ca0L}}}{dt} = -(4\alpha' + \omega)C_{\text{Ca0L}} + \beta'C_{\text{Ca1L}} + \gamma C_{\text{0L}}. \tag{78}$$

$$\frac{dC_{\text{Ca1L}}}{dt} = -\left(3\alpha' + \beta' + \frac{\omega}{b}\right)C_{\text{Ca1L}} + 4\alpha'C_{\text{Ca0L}}$$
$$+ 2\beta'C_{\text{Ca2L}} + \gamma a C_{\text{1L}}. \tag{79}$$

$$\frac{dC_{\text{Ca2L}}}{dt} = -\left(2\alpha' + 2\beta' + \frac{\omega}{b^2}\right)C_{\text{Ca2L}} + 3\alpha'C_{\text{Ca1L}}$$
$$+ 3\beta'C_{\text{Ca3L}} + \gamma a^2 C_{\text{2L}}. \tag{80}$$

$$\frac{dC_{\text{Ca3L}}}{dt} = -\left(\alpha' + 3\beta' + \frac{\omega}{b^3}\right)C_{\text{Ca3L}} + 2\alpha'C_{\text{Ca2L}}$$
$$+ 4\beta'C_{\text{Ca4L}} + \gamma a^3 C_{\text{3L}}. \tag{81}$$

$$\frac{dC_{\text{Ca4L}}}{dt} = -\left(4\beta' + \frac{\omega}{b^4}\right)C_{\text{Ca4L}} + \alpha'C_{\text{Ca3L}} + \gamma a^4 C_{\text{4L}}. \tag{82}$$

$$\frac{dy_{\text{Ca}}}{dt} = \frac{y_\infty - y}{\tau_y}. \tag{83}$$

$$y_\infty = \frac{0.82}{1 + e^{\frac{V + 28.5}{7.8}}} + 0.18. \tag{84}$$

$$\tau_y = \frac{1}{\frac{0.00653}{0.5 + e^{-V/7.1}} + 0.00512e^{-V/39.8}} \tag{85}$$

$$\bar{I}_{\text{Ca}} = \frac{\bar{P}_{\text{Ca}}}{C_{\text{sc}}} \frac{4VF^2}{RT} \frac{0.001e^{2VF/RT} - 0.341[\text{Ca}^{2+}]_o}{e^{2VF/RT} - 1}. \tag{86}$$

$$I_{\text{Ca}} = \bar{I}_{\text{Ca}}yO_L \tag{87}$$

$$I_{\text{Ca,K}} = \frac{P'_K}{C_{\text{SC}}}yO_L\left(\frac{VF^2}{RT}\frac{[\text{K}^+]_i e^{\frac{VF}{RT}} - [\text{K}^+]_o}{e^{\frac{VF}{RT}} - 1}\right). \tag{88}$$

$$P'_K = \frac{\bar{P}_K}{1 + \frac{\bar{I}_{\text{Ca}}}{I_{\text{Ca,half}}}} \tag{89}$$

See Table 12.

RyR channel

$$\frac{dP_{\text{C1}}}{dt} = -k_a^+[\text{Ca}^{2+}]_{\text{ss}}^n P_{\text{C1}} + k_a^- P_{\text{O1}}. \tag{90}$$

TABLE 12 I_{Ca} parameters

Parameter	Value
f	0.3 ms^{-1}
g	4 ms^{-1}
a	2
b	2
ω	2.5 d^{-3} ms^{-1} mm^{-1}
P_{Ca}	1.7283 d^{-3} cm/s
P_K	3.2018 d^{-6} cm/s
$I_{\text{Ca,half}}$	−0.265 pA/pF

$$\frac{dP_{\text{O1}}}{dt} = k_a^+[\text{Ca}^{2+}]_{\text{ss}}^n P_{\text{C1}} - k_a^- P_{\text{O1}} - k_b^+[\text{Ca}^{2+}]_{\text{ss}}^m P_{\text{O1}}$$
$$+ k_b^- P_{\text{O2}} - k_c^+ P_{\text{O1}} + k_c^- P_{\text{C2}}. \tag{91}$$

$$\frac{dP_{\text{O2}}}{dt} = k_b^+[\text{Ca}^{2+}]_{\text{ss}}^m P_{\text{O1}} - k_b^- P_{\text{O2}}. \tag{92}$$

$$\frac{dP_{\text{C2}}}{dt} = k_c^+ P_{\text{O1}} - k_c^- P_{\text{C2}}. \tag{93}$$

$$J_{\text{rel}} = v_1(P_{\text{O1}} + P_{\text{O2}})([\text{Ca}^{2+}]_{\text{JSR}} - [\text{Ca}^{2+}]_{\text{SS}}). \tag{94}$$

SERCA2a pump

$$f_b = \left(\frac{[\text{Ca}^{2+}]_i}{K_{\text{fb}}}\right)^{N_{\text{fb}}}. \tag{95}$$

$$r_b = \left(\frac{[\text{Ca}^{2+}]_{\text{NSR}}}{K_{\text{rb}}}\right)^{N_{\text{rb}}}. \tag{96}$$

$$J_{\text{up}} = K_{\text{SR}}\left(\frac{v_{\text{maxf}}f_b - v_{\text{maxr}}r_b}{1 + f_b + r_b}\right). \tag{97}$$

See Table 13.

Intracellular Ca^{2+} fluxes

$$J_{\text{tr}} = \frac{[\text{Ca}^{2+}]_{\text{NSR}} - [\text{Ca}^{2+}]_{\text{JSR}}}{\tau_{\text{tr}}}. \tag{98}$$

TABLE 13 SR parameters

Parameter	Value
K_a^+	0.01215 μM^{-4} ms^{-1}
K_a^-	0.576 ms^{-1}
K_b^+	0.00405 μM^{-3} ms^{-1}
K_b^-	1.93 ms^{-1}
K_c^+	0.3 ms^{-1}
K_c^-	0.0009 ms^{-1}
v_1	1.8 ms^{-1}
K_{fb}	0.000168 mM
N_{fb}	1.2
K_{rb}	3.29 mM
N_{rb}	1
v_{maxf}	0.0748 d^{-3} mM/ms
v_{maxr}	0.03748 d^{-3} mM/ms
K_{SR}	1.2

$$J_{xfer} = \frac{[Ca^{2+}]_{ss} - [Ca^{2+}]_i}{\tau_{xfer}}. \quad (99)$$

$$J_{trpn} = \frac{d[HTRPN_{Ca}]}{dt} + \frac{d[LTRPN_{Ca}]}{dt}. \quad (100)$$

$$\frac{d[HTRPN_{Ca}]}{dt} = k_{htrpn}^+[Ca^{2+}]_i([HTRPN]_{tot} - [HTRPN_{Ca}]) - k_{htrpn}^-[HTRPN_{Ca}]. \quad (101)$$

$$\frac{d[LTRPN_{Ca}]}{dt} = k_{ltrpn}^+[Ca^{2+}]_i([LTRPN]_{tot} - [LTRPN_{Ca}]) - k_{ltrpn}^-[LTRPN_{Ca}]. \quad (102)$$

See Table 14.

Intracellular ion concentrations and membrane potential

$$\frac{d[Na^+]_i}{dt} = -(I_{Na} + I_{Na,b} + 3I_{NaCa} + 3I_{NaK} + I_{Kv1.4,Na})\frac{A_{cap}C_{sc}}{V_{myo}F}. \quad (103)$$

$$\frac{d[K^+]_i}{dt} = -(I_{Kr} + I_{Ks} + I_{Kv4.3} + I_{Kv1.4,K} + I_{K1} + I_{Ca,K} - 2I_{NaK} + I_{stim})\frac{A_{cap}C_{sc}}{V_{myo}F}. \quad (104)$$

$$\frac{d[Ca^{2+}]_i}{dt} = \beta_i\left(J_{xfer} - J_{up} - J_{trpn} - (I_{Ca,b} - 2I_{NaCa} + I_{p(Ca)})\right. \times \left.\frac{A_{cap}C_{sc}}{2V_{myo}F}\right). \quad (105)$$

$$\beta_i = \left(1 + \frac{[CMDN]_{tot}K_m^{CMDN}}{(K_m^{CMDN} + [Ca^{2+}]_i)^2} + \frac{[EGTA]_{tot}K_m^{EGTA}}{(K_m^{EGTA} + [Ca^{2+}]_i)^2}\right). \quad (106)$$

$$\beta_{ss} = \left(1 + \frac{[CMDN]_{tot}K_m^{CMDN}}{(K_m^{CMDN} + [Ca^{2+}]_{ss})^2} + \frac{[EGTA]_{tot}K_m^{EGTA}}{(K_m^{EGTA} + [Ca^{2+}]_{ss})^2}\right). \quad (107)$$

TABLE 14 Calcium buffering and diffusion

Parameter	Value
τ_{tr}	0.5747 ms
τ_{xfer}	26.7 ms
$HTRPN_{tot}$	140 d^{-3} mM
$LTRPN_{tot}$	70 d^{-3} mM
K_{HTRPN}^+	20 mM^{-1} ms^{-1}
K_{HTRPN}^-	0.066 d^{-3} ms^{-1}
K_{LTRPN}^+	40 mM^{-1} ms^{-1}
K_{LTRPN}^-	40 d^{-3} ms^{-1}
K_m^{CMDN}	2.38 d^{-3} mM
K_m^{CSQN}	0.8 mM
K_m^{EGTA}	1.5 d^{-4} mM
$EGTA_{tot}$	0 mM

$$\beta_{JSR} = \left(1 + \frac{[CSQN]_{tot}K_m^{CSQN}}{(K_m^{CSQN} + [Ca^{2+}]_{JSR})^2}\right)^{-1}. \quad (108)$$

$$\frac{d[Ca^{2+}]_{ss}}{dt} = \beta_{ss}\left(J_{rel}\frac{V_{JSR}}{V_{ss}} - J_{xfer}\frac{V_{myo}}{V_{ss}} - (I_{Ca})\frac{A_{cap}C_{sc}}{2V_{ss}F}\right). \quad (109)$$

$$\frac{d[Ca^{2+}]_{JSR}}{dt} = \beta_{JSR}(J_{tr} - J_{rel}). \quad (110)$$

$$\frac{d[Ca^{2+}]_{NSR}}{dt} = J_{up}\frac{V_{myo}}{V_{NSR}} - J_{tr}\frac{V_{JSR}}{V_{NSR}}. \quad (111)$$

$$\frac{dV}{dt} = -(I_{Na} + I_{Ca} + I_{Ca,K} + I_{Kr} + I_{Ks} + I_{K1} + I_{NaCa} + I_{NaK} + I_{Kv1.4} + I_{Kv4.3} + I_{p(Ca)} + I_{Ca,b} + I_{Na,b} + I_{stim}). \quad (112)$$

$$I_{stim} = -100\,pA/pF. \quad (113)$$

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